

# Nuclear Structure in Exotic Nuclei : From $^{100}\text{Sn}$ to $^{78}\text{Ni}$

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## TOPICS:

### Techniques:

- in-beam
- ISOL
- in-flight separation

### $N \simeq Z$ ( $^{100}\text{Sn}$ ):

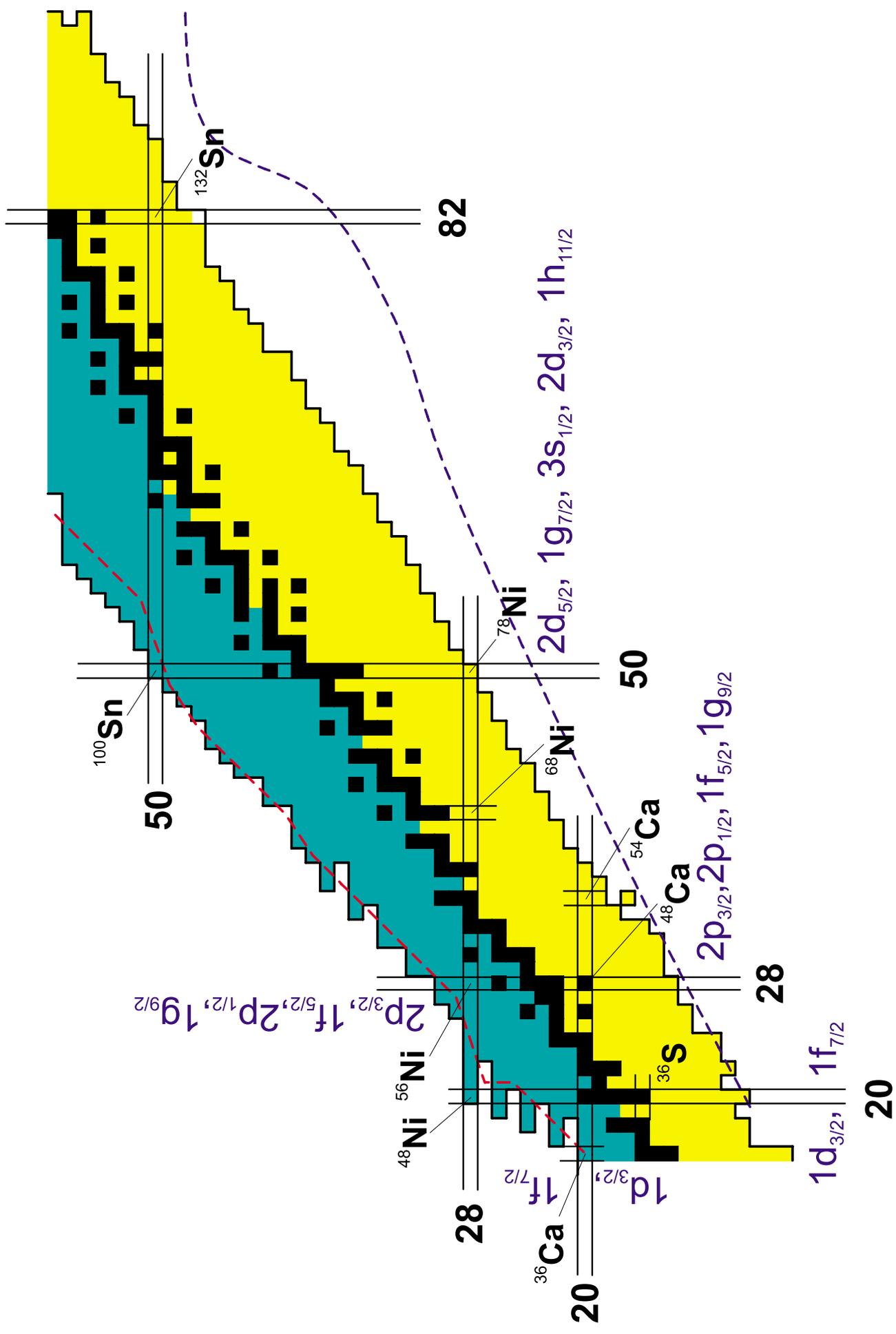
- single particle energies
- core excitation  $L = 2, (3, \sigma, \sigma\tau)$
- $\pi\nu$  interaction; seniority vs. spin-gap isomers
- empirical vs. large-scale shell model

### $N \gg Z$ ( $^{68-78}\text{Ni}$ ):

- monopole interaction
- $\sigma\tau$  vs.  $(\sigma \times \vec{r})\tau$  driven shell structure
- $N=40$  and  $50$  shell evolution

### New shells @ $N \gg Z$ :

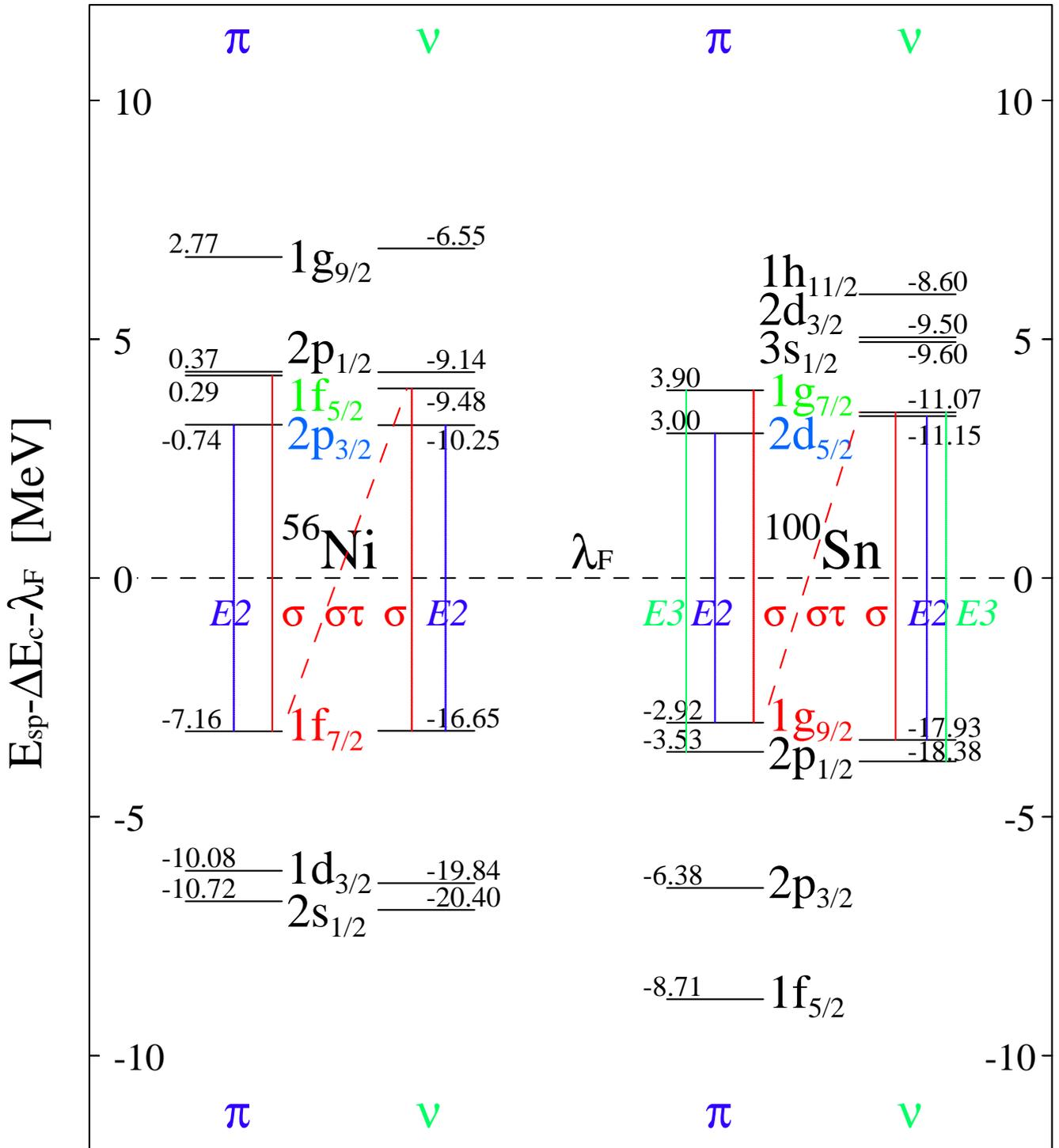
- harmonic oscillator vs. spin-orbit shell
- $N=6, 16(14), 34(32)$  examples
- $T=1$  monopole



# Shell structure in $N = Z$ doubly magic

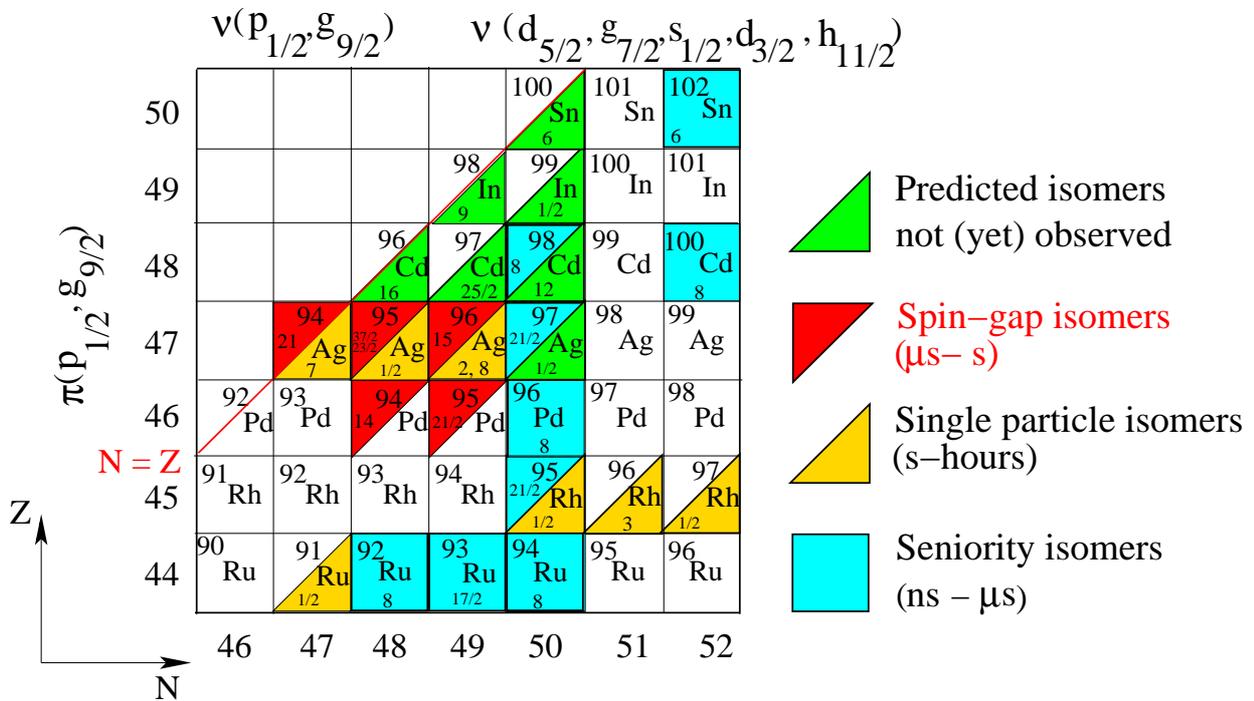


and



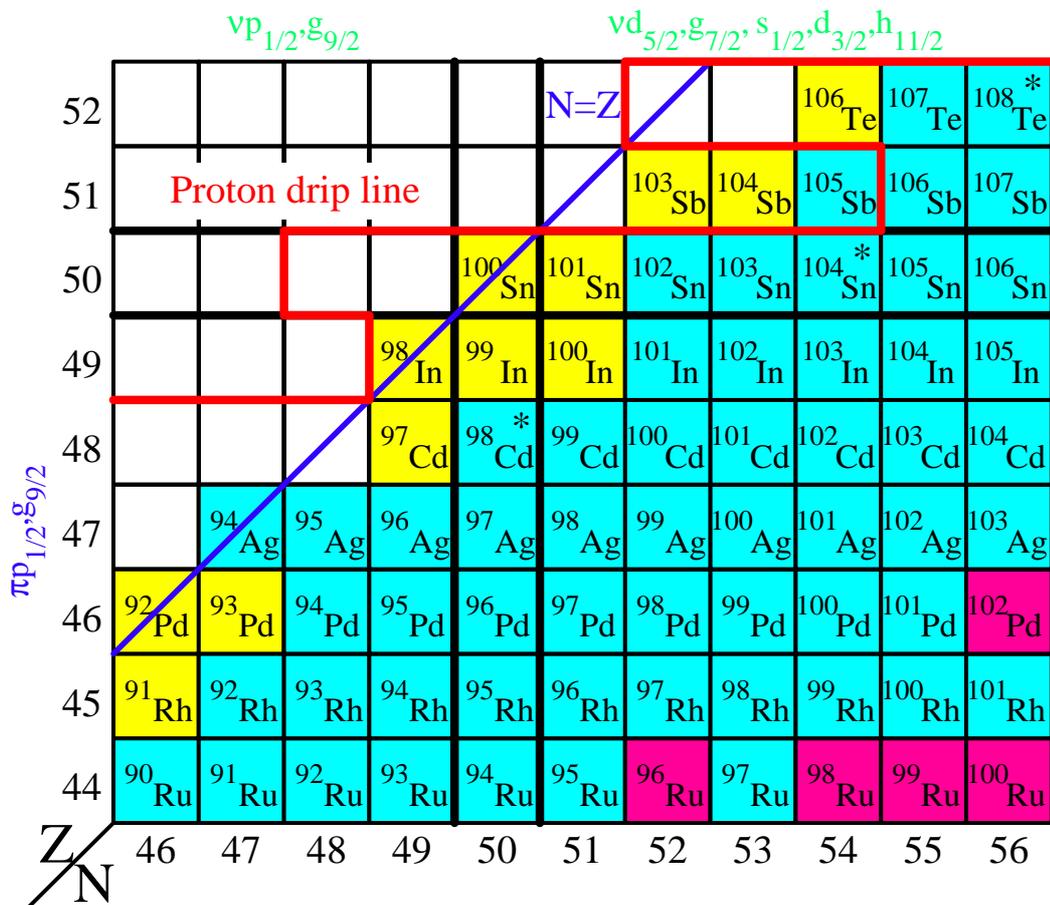
o  $L=2$  ( $=|l_p - l_n|$ ) softness,  $E2$  polarisation, isomers  
o  $\sigma/M1$  and  $\sigma\tau/GT$  transitions  
o  $L=3$  ( $=|l_p \pm l_n|$ )  $E3$  collectivity

Isomer landscape around  $^{100}\text{Sn}$



## Experimental approach to $^{100}\text{Sn}$

- o in-beam, fusion-evaporation
- o ISOL mass separation, fusion-evaporation
- o in-flight A,Z separation, fragmentation



- Nucleus produced in an experiment
- Nucleus with known excited states
- Stable nucleus

## Shell model $^{100}\text{Sn}$ np - nh in gds space

*F. Nowacki, NPA704,223c(02)*

$$\begin{aligned}
 {}^{98}\text{Cd} \text{ B(E2; } 8^+ \rightarrow 6^+) &= 37 e^2 fm^4 & \mathbf{0p - 0h} \\
 &= 57 e^2 fm^4 & \mathbf{4p - 4h} \\
 &= 14 \binom{7}{4} e^2 fm^4 & \mathbf{Exp}^a \\
 &= 30(4) e^2 fm^4 & \mathbf{Exp}^b \\
 &\rightarrow \delta e_\pi \sim 0.1e
 \end{aligned}$$

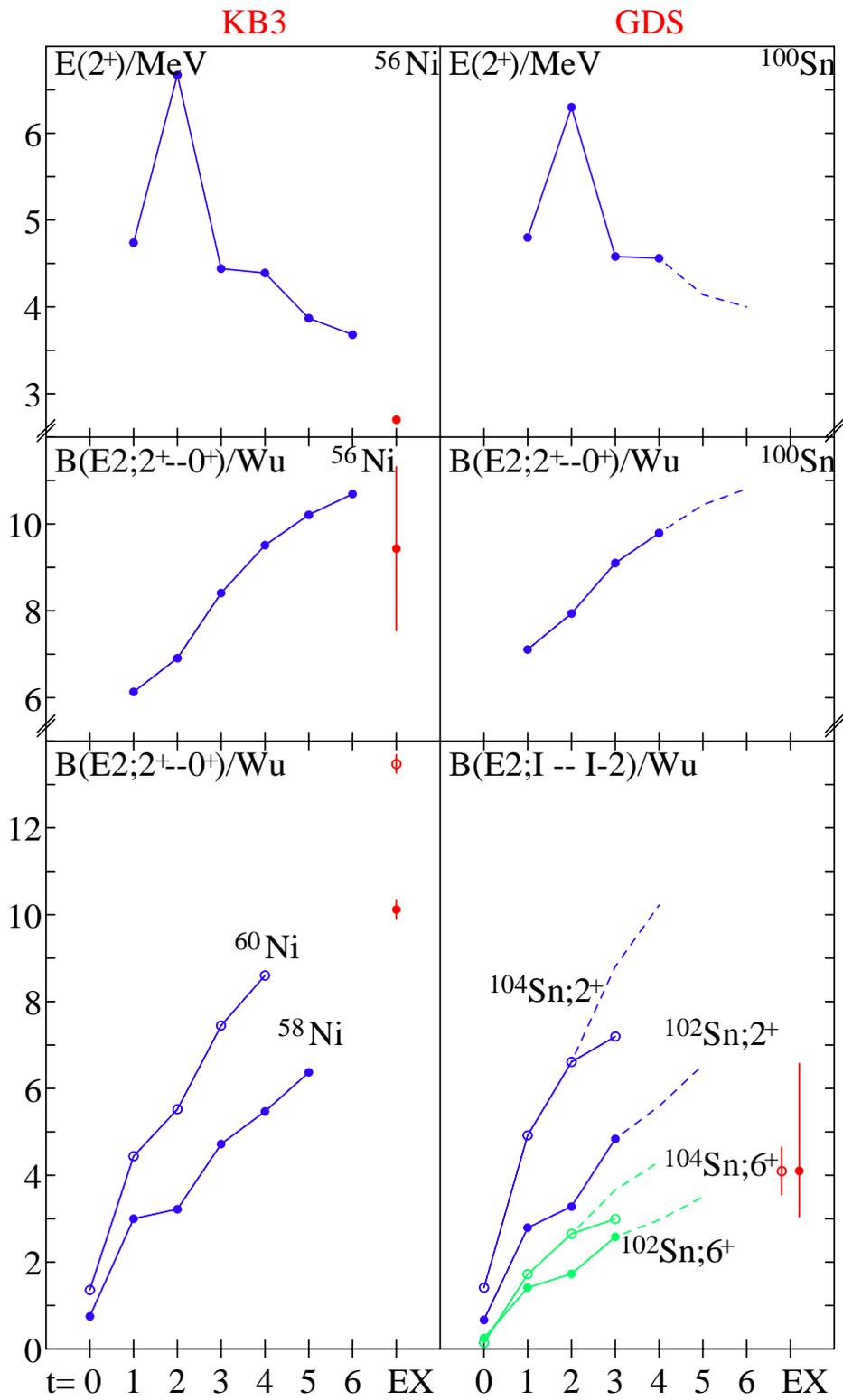
$$\begin{aligned}
 {}^{102}\text{Sn} \text{ B(E2; } 6^+ \rightarrow 4^+) &= 7.2 e^2 fm^4 & \mathbf{0p - 0h} \\
 &= 73 e^2 fm^4 & \mathbf{3p - 3h} \\
 &= 116 \binom{70}{30} e^2 fm^4 & \mathbf{Exp}^c \\
 &\rightarrow \delta e_\nu \sim 0.6e
 \end{aligned}$$

**Large Isovector Effect !**

<sup>a</sup> M. Górska et al., PRL 79, 2415 (1997)

<sup>b</sup> R. Grzywacz, ENAM98, AIP Conf. Proc. 455, 430 (1998)

<sup>c</sup> M. Lipoglavšek et al., PL 440B, 246 (1998)



# $^{100}\text{Sn}$ core excitation

<sup>a</sup> M. Górska et al., PRL 79,2415(1997)

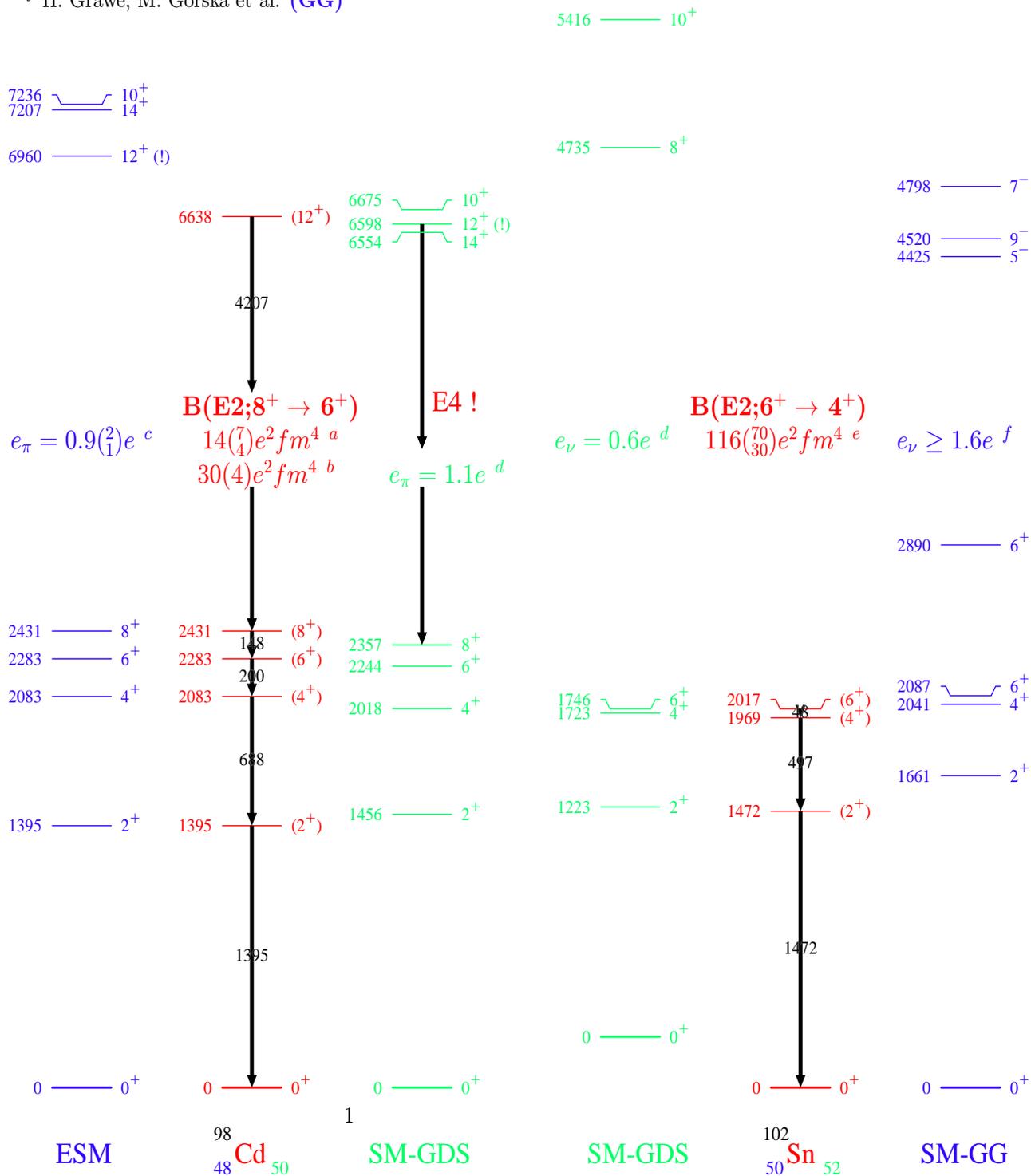
<sup>b</sup> R. Grzywacz, ENAM98, AIP CP 455,430(1998)

<sup>c</sup> H. Grawe et al., NS98, AIP CP 481,177(1999) (ESM)

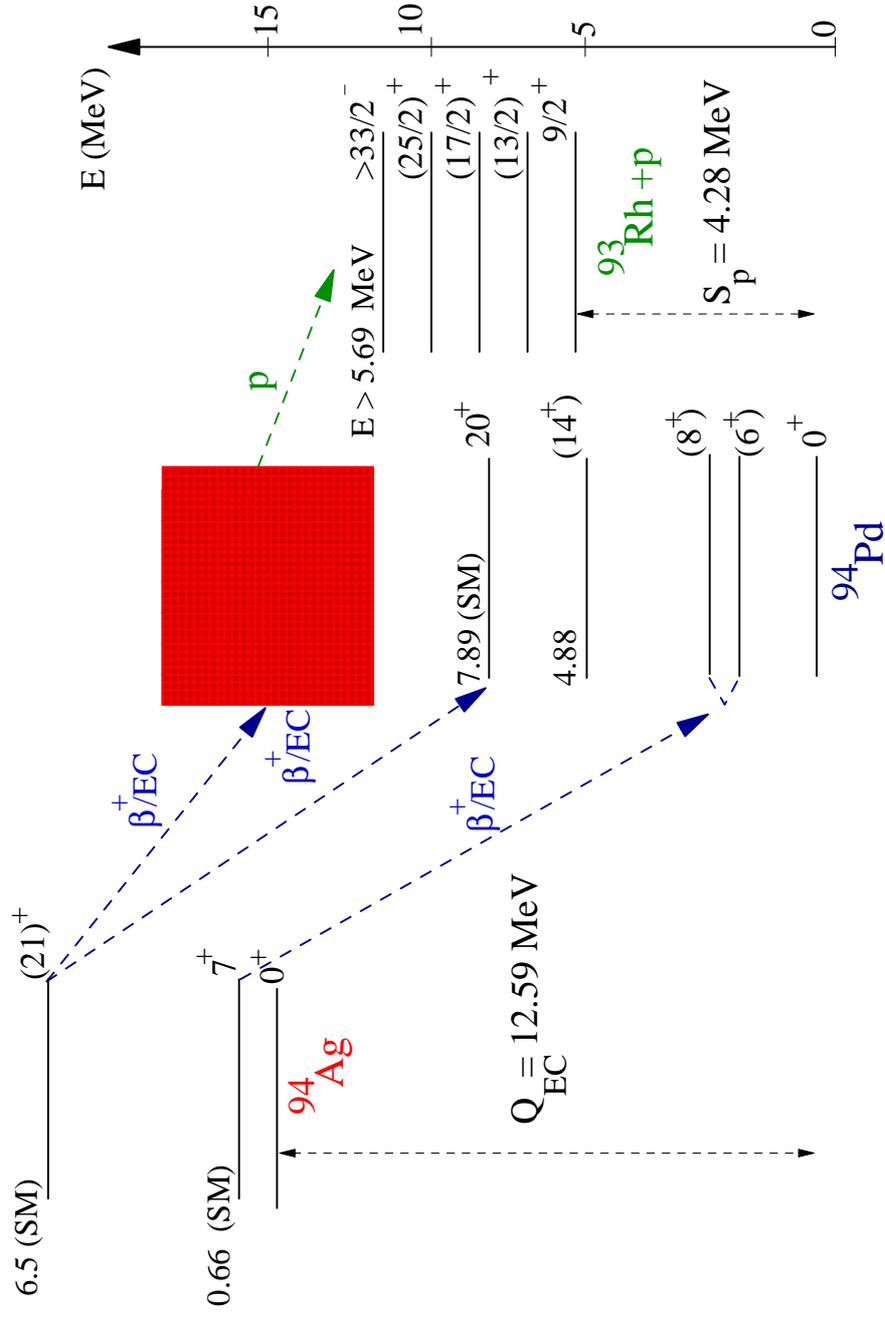
<sup>d</sup> F. Nowacki, NPA704,223c(2002) (GDS)

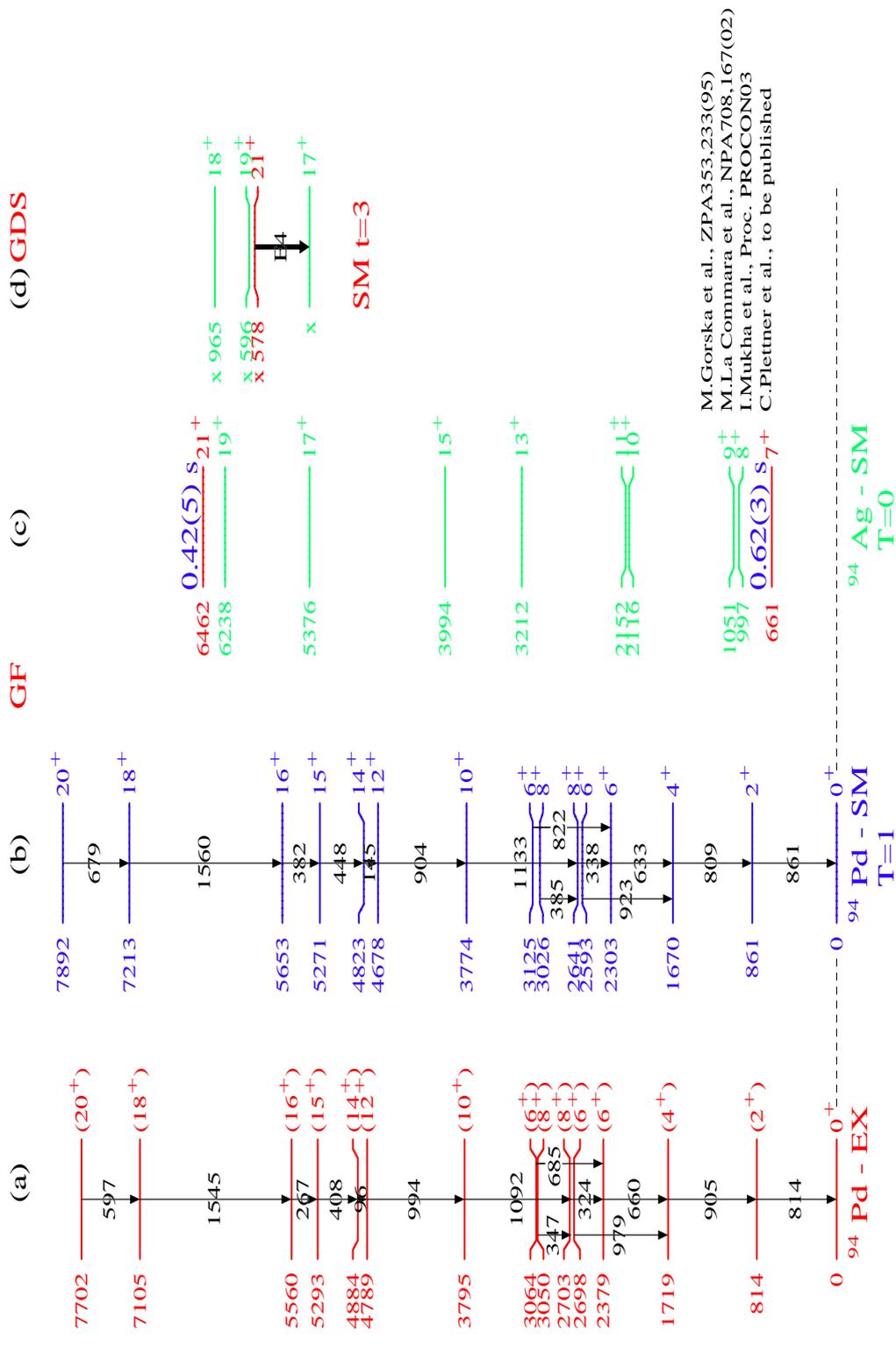
<sup>e</sup> M. Lipoglavšek et al., ZPA356,239(1996); PLB440,246(1998)

<sup>f</sup> H. Grawe, M. Górska et al. (GG)

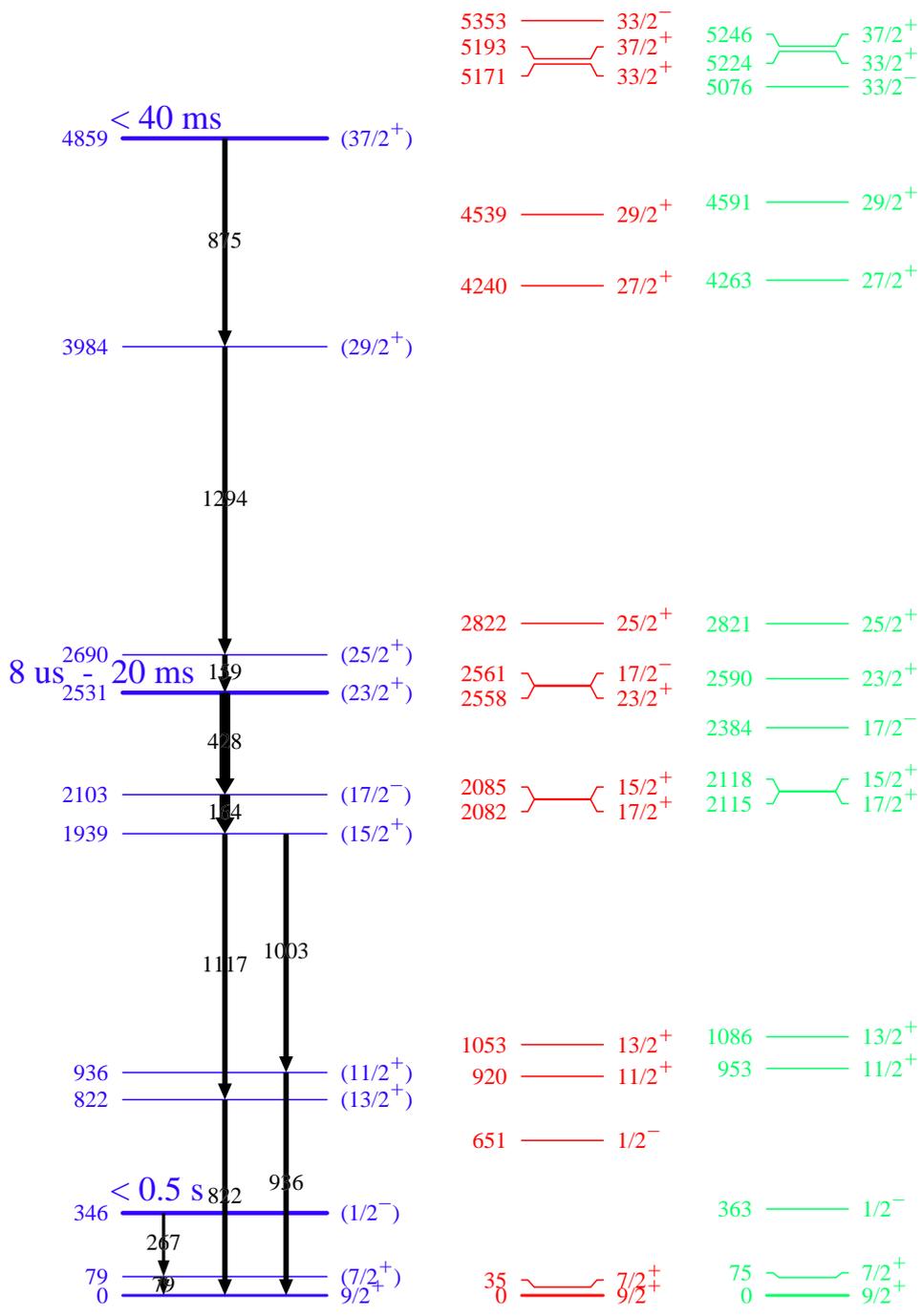


# The decay modes of $^{94}\text{Ag}$





M. Gorska et al., ZPA353.233(95)  
 M. La Commara et al., NPA708.167(02)  
 I. Mukha et al., Proc. PROCON03  
 C. Pletner et al., to be published



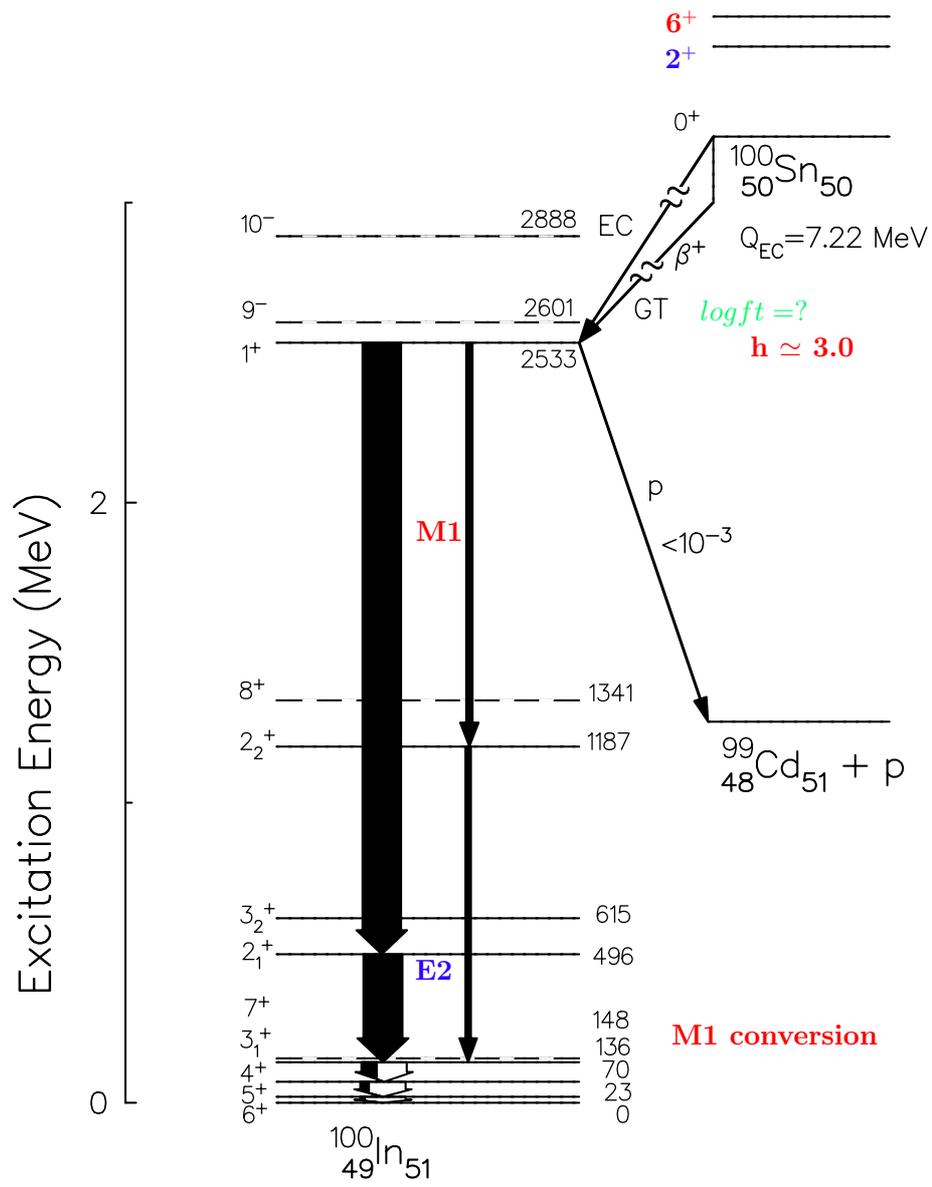
EX

SM-GF

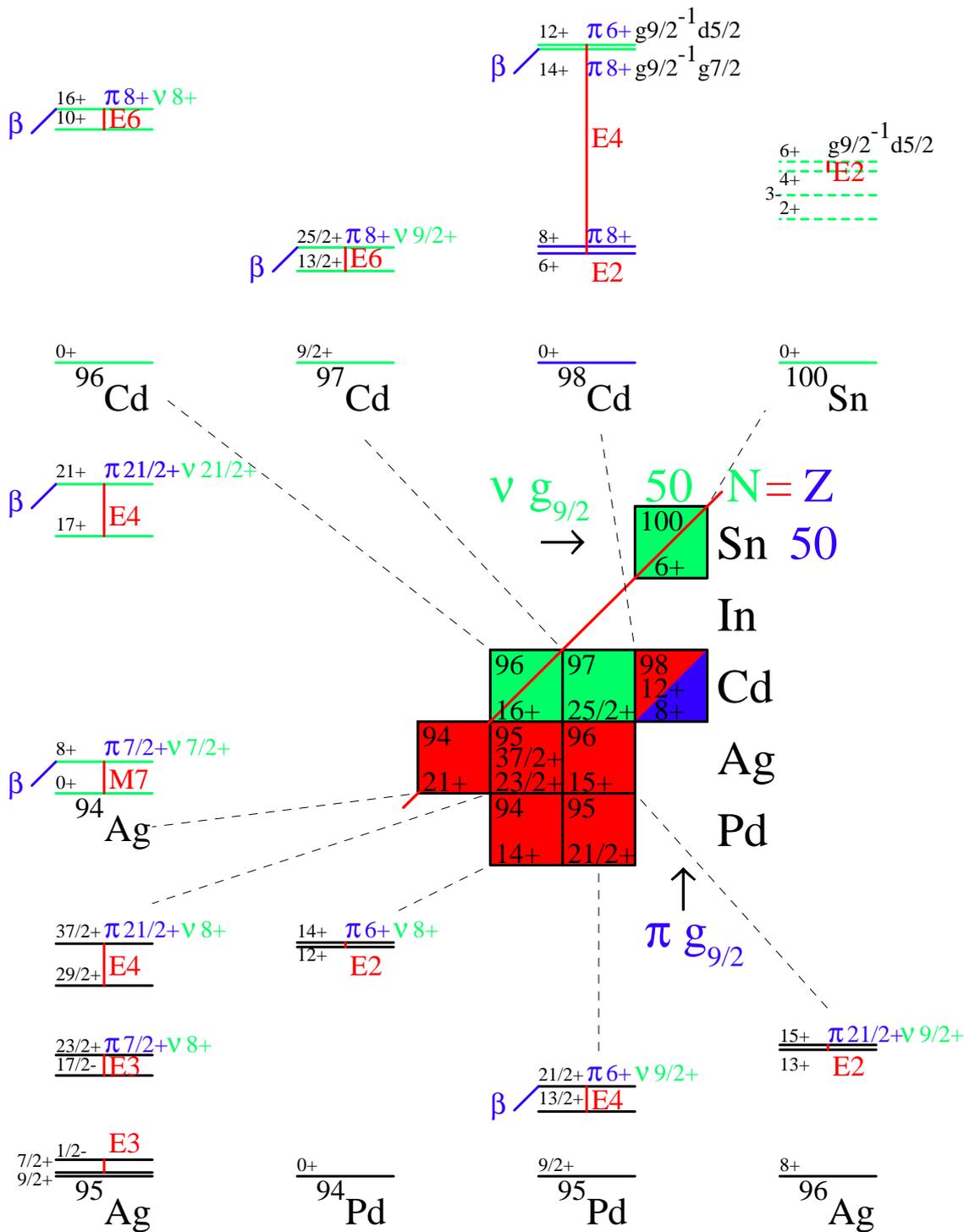
SM-GFP

$^{95}\text{Ag}_{48}$

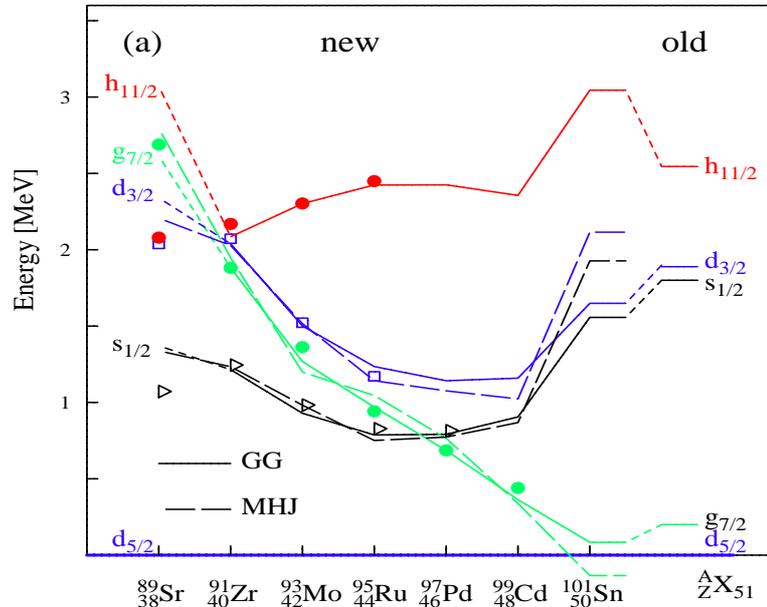
# $^{100}\text{Sn}$ $\beta^+/\text{EC}$ decay



## Spin gap isomers below $N=Z=50$

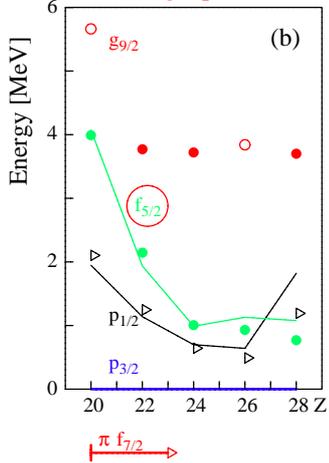


**N=51 Single particle states**

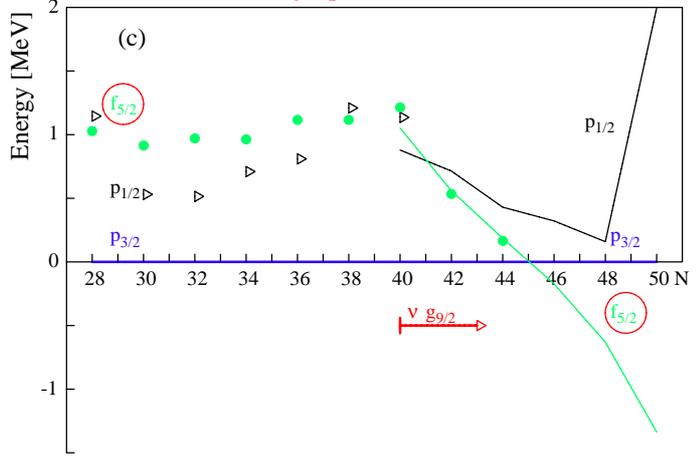


$\pi g_{9/2}$

**N=29 Single particle states**



**Z=29 Single particle states**



**Monopole strong for :**

- $\rightarrow \pi \nu (T=0)$  proton-neutron interaction
- $\rightarrow S = 0$  spin-flip
- $\rightarrow n_1 = n_2$  radial overlap



## MONOPOLE SHIFT – REALISTIC INTERACTION

**Monopole:**

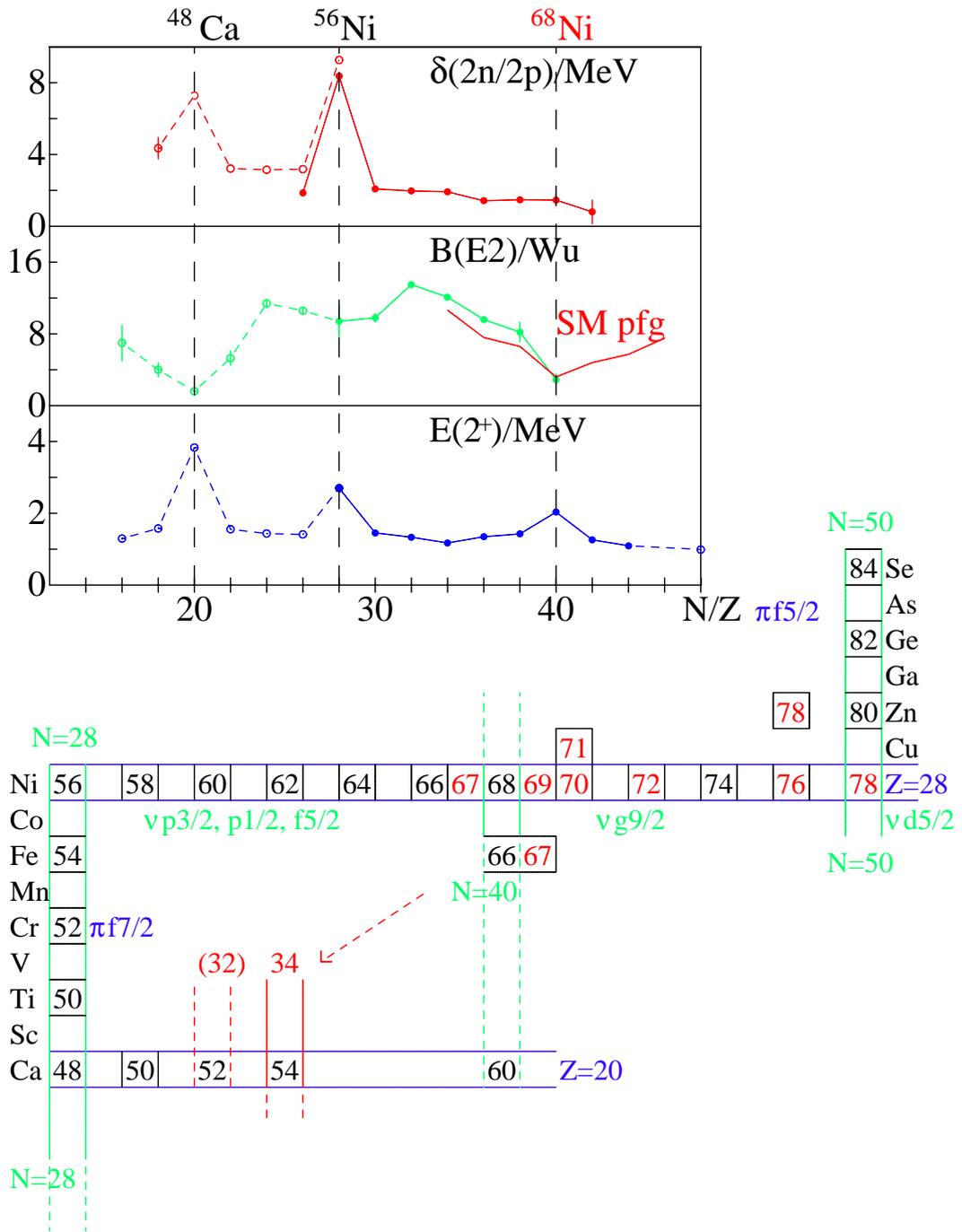
$$V_{jj'}^m = \Sigma_J(2J + 1) \langle jj' | V | jj' \rangle_J / \Sigma_J(2J + 1)$$

**Relative orbital monopole shift:**

$$\Delta(j'_1, j'_2) = V_{jj'_1}^m \cdot (2j + 1 - \delta_{jj'_1}) - V_{jj'_2}^m \cdot (2j + 1 - \delta_{jj'_2})$$

Multiplet $j, j'_{1,2}$	S,T/ $\pi\nu$	$V^m$ (MeV)	$\Delta(j'_1, j'_2)$ (MeV)	Interaction
$\pi f_{7/2} \nu f_{5/2}$	<b>S=0, <math>\pi\nu</math></b>	<b>-1.046</b>	<b>4.258</b>	<b>FPD6</b>
$\pi f_{7/2} \nu p_{3/2}$	<b>S=1, <math>\pi\nu</math></b>	<b>-0.513</b>		<b>NPA523(91)325</b>
$f_{7/2} f_{5/2}$	<b>S=0, T=1</b>	<b>-0.082</b>		
$f_{7/2} p_{3/2}$	<b>S=1, T=1</b>	<b>+0.174</b>		
$f_{7/2}^2$	<b>S=1, T=1</b>	<b>-0.208</b>		
$\pi f_{7/2} \nu f_{5/2}$	<b>S=0, <math>\pi\nu</math></b>	<b>-1.134</b>	<b>4.352</b>	<b>KB</b>
$\pi f_{7/2} \nu p_{3/2}$	<b>S=1, <math>\pi\nu</math></b>	<b>-0.590</b>		<b>NPA114(68)241</b>
$f_{7/2} f_{5/2}$	<b>S=0, T=1</b>	<b>-0.464</b>		
$f_{7/2} p_{3/2}$	<b>S=1, T=1</b>	<b>-0.251</b>		
$f_{7/2}^2$	<b>S=1, T=1</b>	<b>-0.301</b>		
$\nu g_{9/2} \pi f_{5/2}$	<b>S=0, <math>\pi\nu</math></b>	<b>-1.034</b>	<b>5.310</b>	<b>S3V68</b>
$\nu g_{9/2} \pi p_{3/2}$	<b>S=1, <math>\pi\nu</math></b>	<b>-0.503</b>		<b>J.Phys.G18</b>
$g_{9/2} f_{5/2}$	<b>S=0, T=1</b>	<b>-0.504</b>		<b>(92)1377,1401</b>
$g_{9/2} p_{3/2}$	<b>S=1, T=1</b>	<b>-0.123</b>		
$g_{9/2}^2$	<b>S=1, T=1</b>	<b>-0.134</b>		
$\pi g_{9/2} \nu g_{7/2}$	<b>S=0, <math>\pi\nu</math></b>	<b>-0.744</b>	<b>4.258</b>	<b>MHJ</b>
$\pi g_{9/2} \nu d_{5/2}$	<b>S=1, <math>\pi\nu</math></b>	<b>-0.370</b>		<b>Phys.Rep.261</b>
$g_{9/2}^2$	<b>S=1, T=1</b>	<b>-0.098</b>		<b>(95)125</b>

# From N=28 to N=50



## N = 50 shell gap extrapolation

**Configurations:**  $\pi 0 f_{5/2} \nu 0 g_{9/2}$   
 $\pi 0 f_{5/2} \nu 1 d_{5/2}$

**Assumption:**  $V_{f_{5/2}d_{5/2}}^m \approx 0.5 \cdot V_{f_{5/2}g_{9/2}}^m$

	$Z=28$	$N = 50$	shell gap	
	<i>occ.</i>	<i>SkP/HFB</i>	<i>EXP</i>	
	$\pi 0 f_{5/2}$	(MeV)	(MeV)	
<i>Se</i>	6	2.8	4.13(4)	
<i>Ge</i>	4	2.5	3.8(4)	
<i>Zn</i>	2	2.0	-	
<i>Ni</i>	0	1.9	<b>2.08</b>	<i>S3V68</i>
			<b>2.60</b>	<i>S3V</i>
			<b>2.56</b>	"EXP"

## Z = 28 shell gap extrapolation

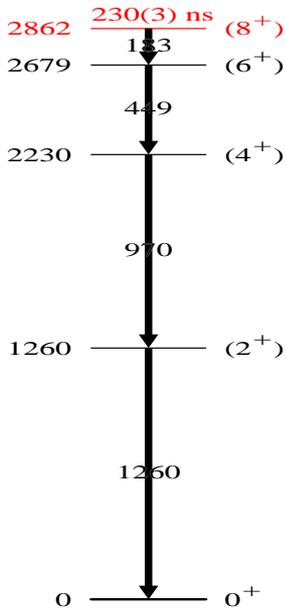
**Configurations:**  $\pi 0 f_{5/2} \nu 0 g_{9/2}$   
 $\pi 0 f_{7/2} \nu 0 g_{9/2}$

**Assumption:**  $V_{f_{7/2}g_{9/2}}^m \approx 0.5 \cdot V_{f_{5/2}g_{9/2}}^m$

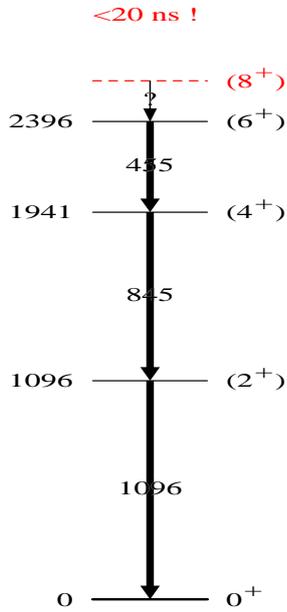
$N=40$	$Z = 28$	shell gap	
<i>occ.</i>		<i>EXP</i>	
$\nu 0 g_{9/2}$		(MeV)	
0		5.91(28)	
10		<b>4.46</b>	<b>S3V68</b>
		<b>4.39</b>	<b>S3V</b>
		<b>3.58</b>	"EXP"

# I<sup>π</sup>=8<sup>+</sup> isomerism

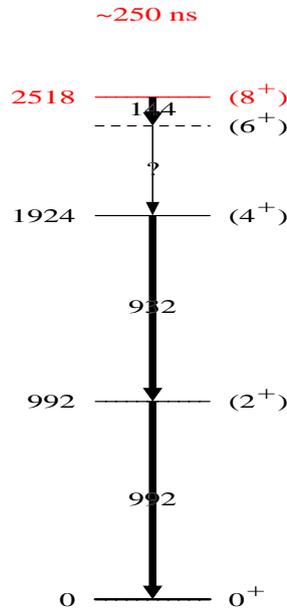
<sup>72</sup>Co<sub>27</sub><sup>45</sup> (6,7)<sup>-</sup>



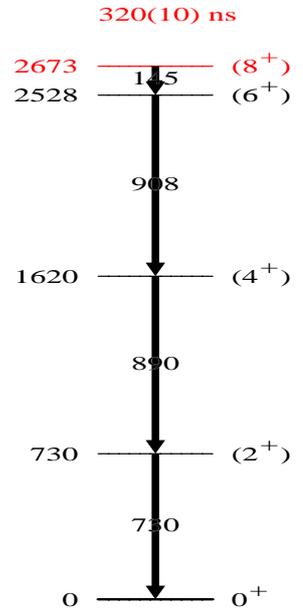
<sup>70</sup>Ni<sub>28</sub><sup>42</sup>



<sup>72</sup>Ni<sub>28</sub><sup>44</sup>

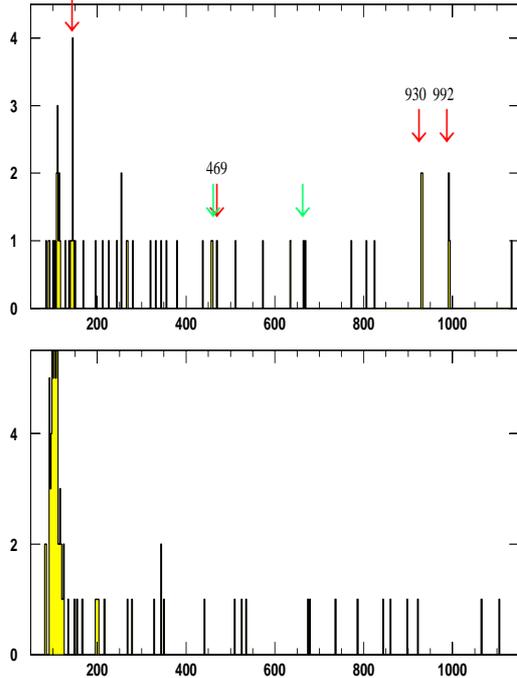


<sup>76</sup>Ni<sub>28</sub><sup>48</sup>

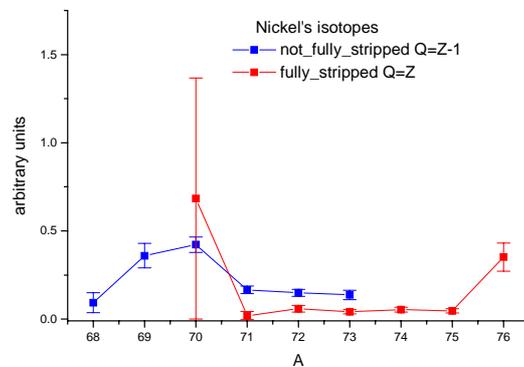


<sup>78</sup>Zn<sub>30</sub><sup>48</sup>

<sup>76</sup>Ni following fragmentation of 58 MeV/A <sup>86</sup>Kr at GANIL



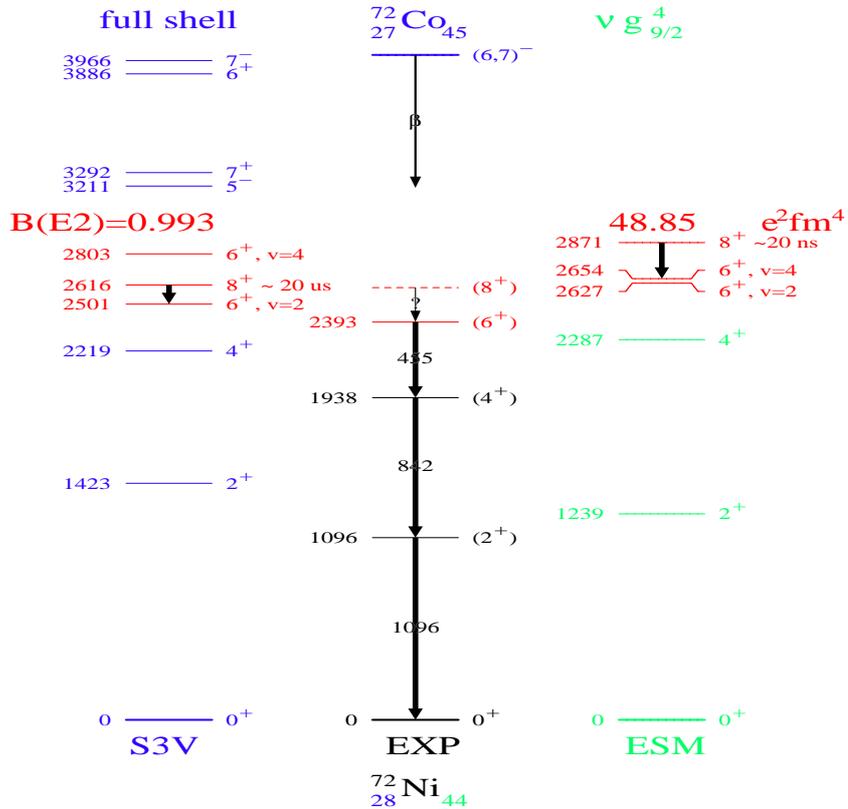
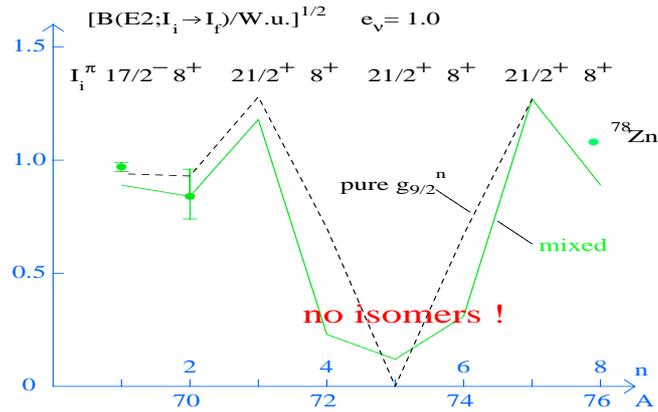
"Isomeric ratio"



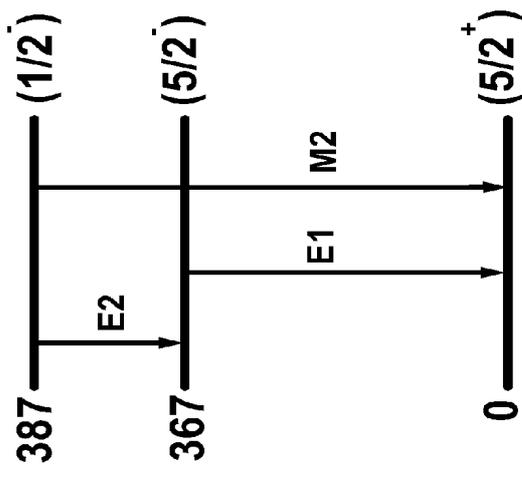
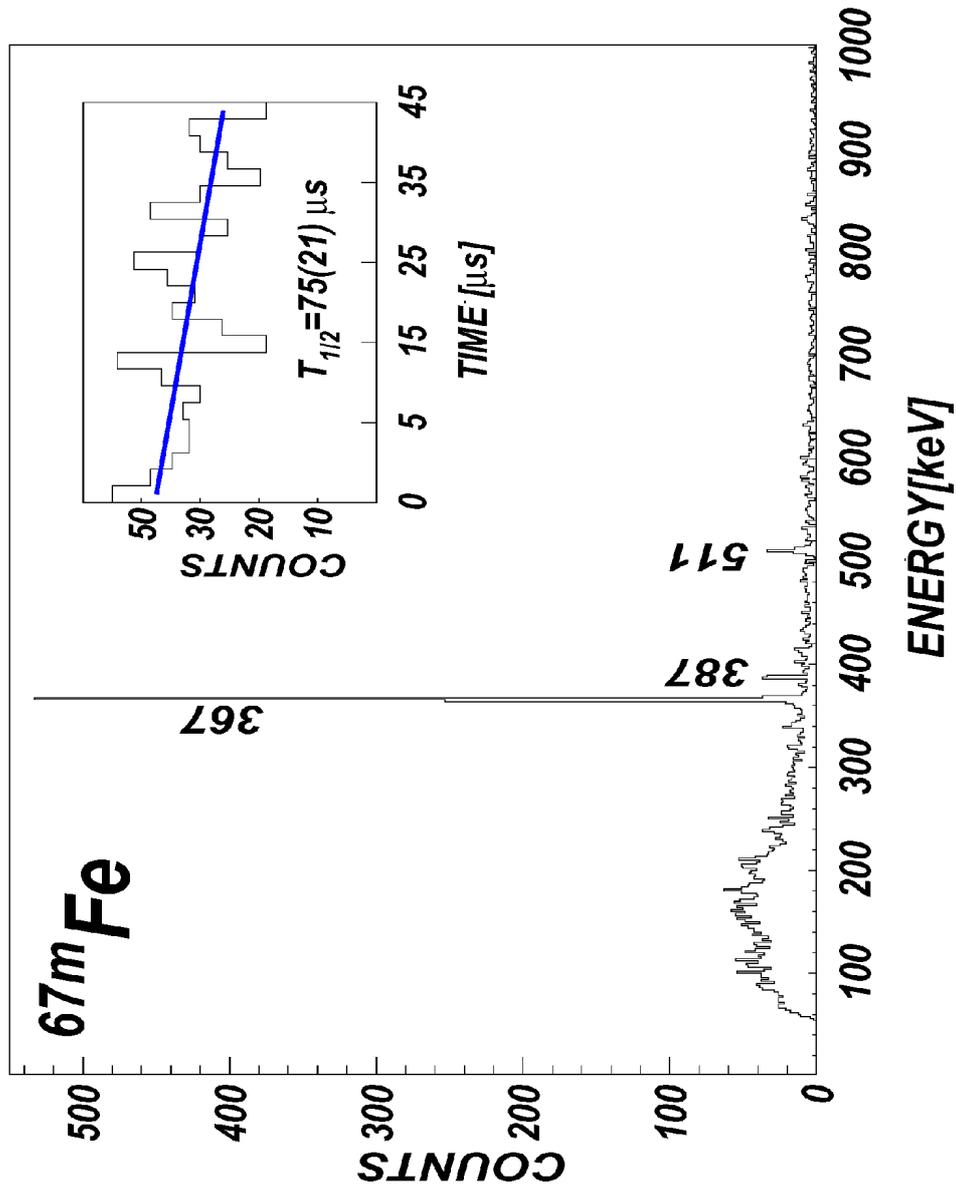
# Missing $I^\pi=8^+$ isomer

## Seniority isomers

### E2 transitions in $N > 40$ Ni isotopes



M. Sawicka et al.: New evidence for the isomeric decay of  $^{67}\text{Fe}$

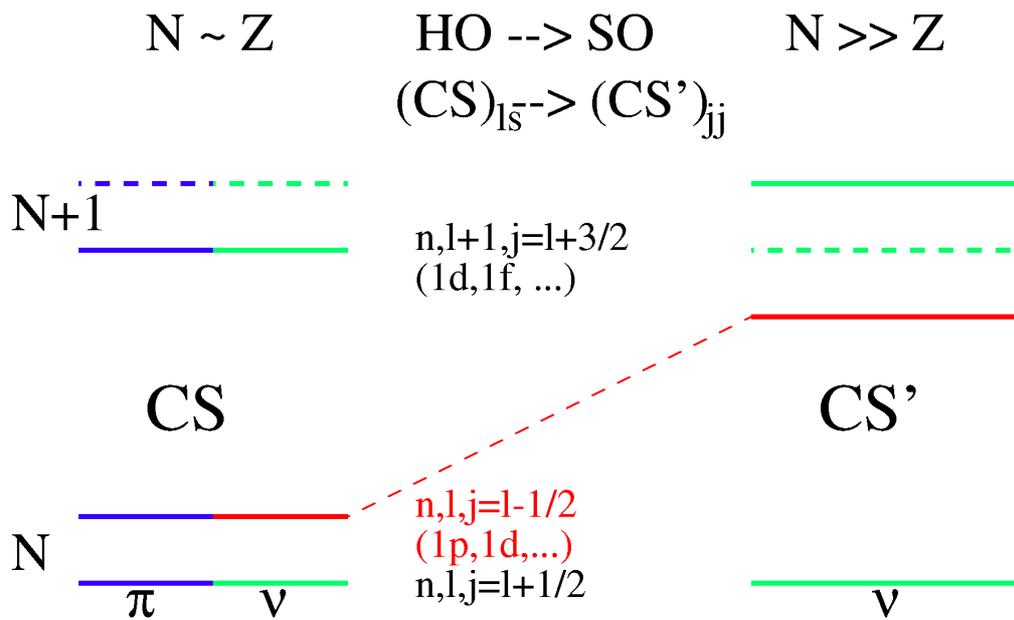


## Monopole migration

$$V^m = \frac{\sum (2J+1) \langle jj' | V | jj' \rangle}{\sum (2J+1)}$$

$$V = - |v_{\sigma\tau}(r)| (\sigma \sigma)(\tau \tau)$$

$$\left. \begin{array}{l} S=1 : \sim 1 \\ S=0 : \sim 2 \end{array} \right\} \begin{array}{l} T=1 : =1 \\ T=0 : =3 \end{array} \} \pi v \sim 2$$



**Signature:**

- HO (ls) --> SO (jj) shell
- rapid change, locality
- SO splitting increased (apparent)

$N_m^- \rightarrow N_m^-$	$2 * N$
8	6
20	16(14)
40	34(32)

# Tensor monopole interaction

(T. Otsuka, private communication)

$$V^m = \frac{\sum (2J+1) \langle jj' | V | jj' \rangle_j}{\sum (2J+1)}$$

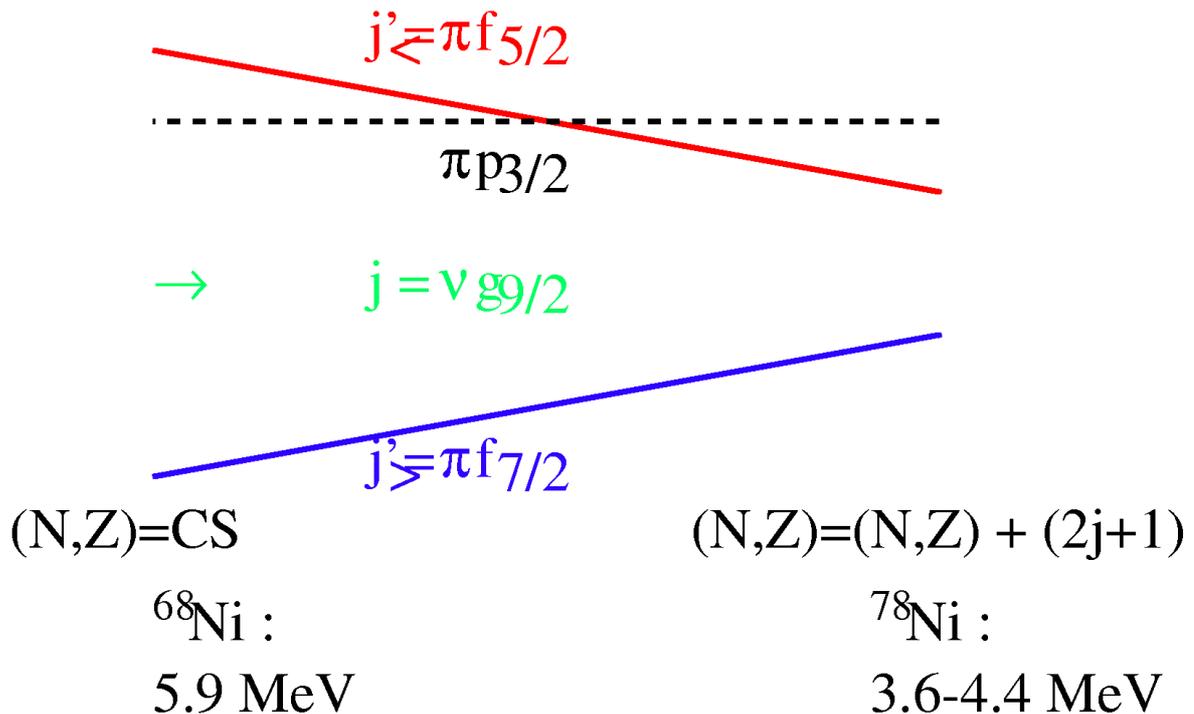
$$V = v_T(r) (\sigma \cdot r) (\sigma \cdot r) (\tau \cdot \tau)$$

$$\rightarrow \sim (\sigma \cdot Y^1)^k$$

Strong for  $k=2$  and  $\pi v$

Sum rule :

$$\sum (2J+1) \langle jj' | V | jj' \rangle_{\leftarrow} + \sum (2J+1) \langle jj' | V | jj' \rangle_{\rightarrow} = 0$$



Signature:

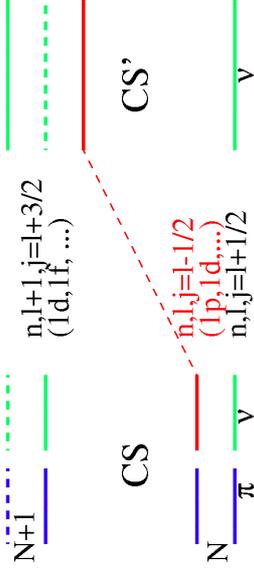
-- rapid change, locality

-- SO splitting reduced

(apparent)

$N \sim Z$        $HO \rightarrow SO$        $N \gg Z$

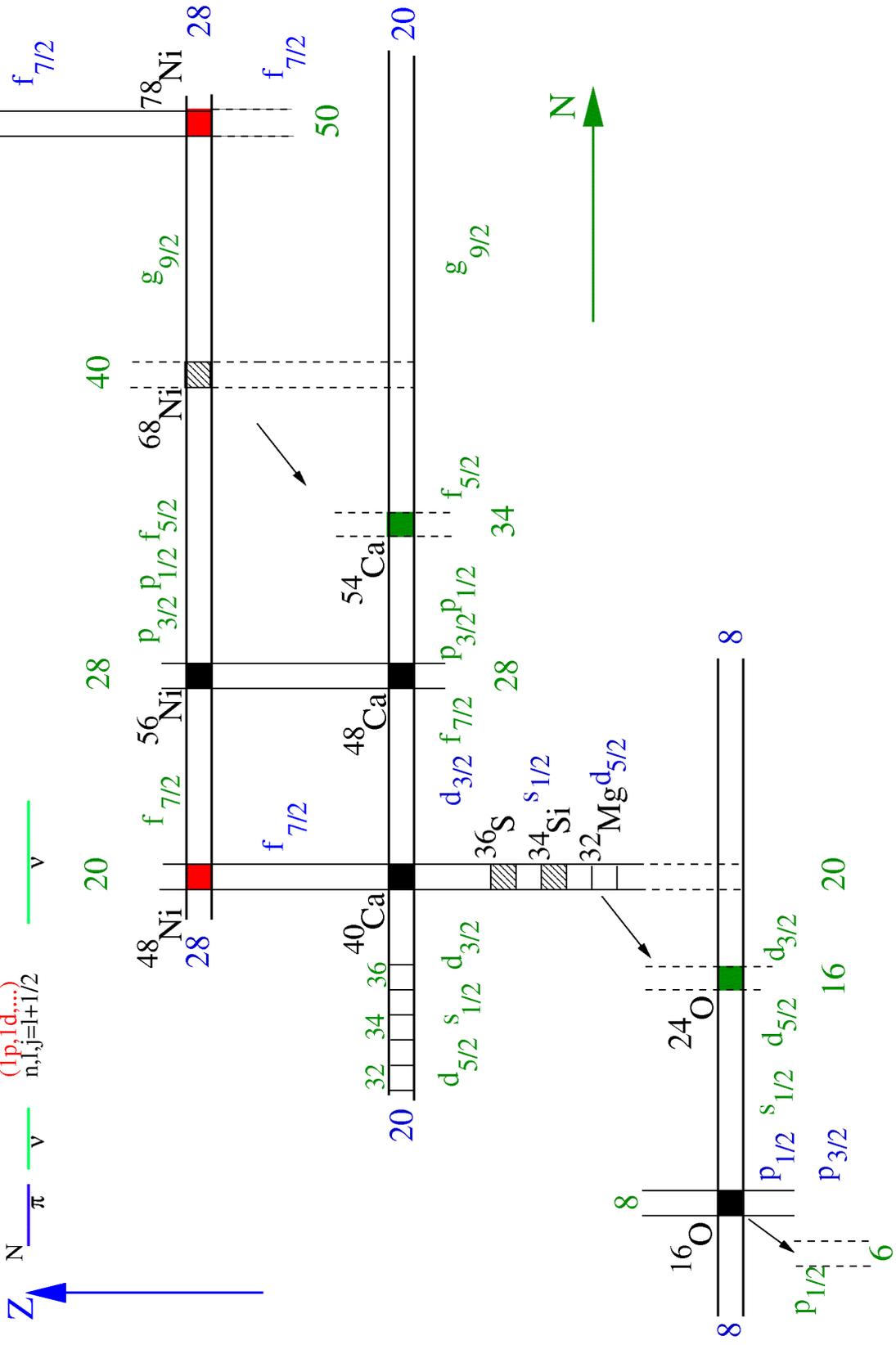
$(CS)_{IS} \rightarrow (CS')_{jj}$



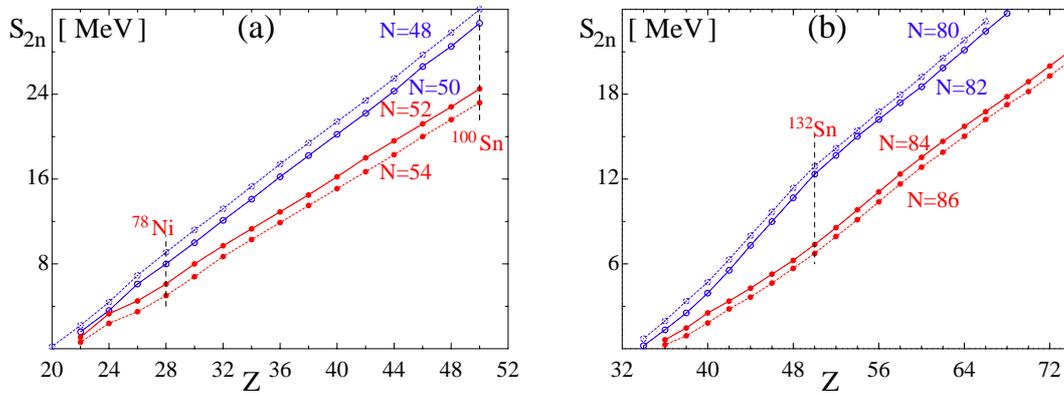
$n, l, j = l-1/2$   
( $1p, 1d, \dots$ )  
 $n, l, j = l+1/2$

# New shells :

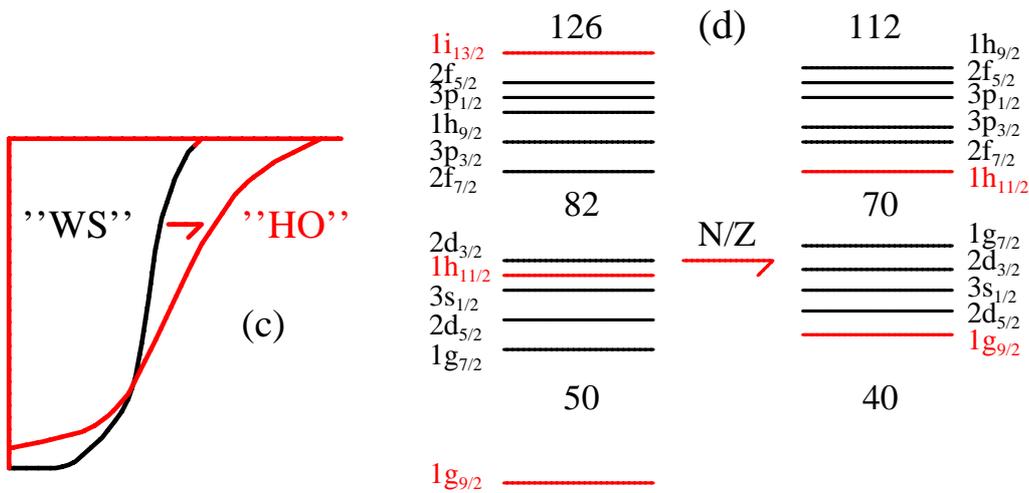
$$n_{\text{new}} = n_{\text{old}} + 2 * N$$



# Shell quenching



# New shells



# Signature

- **Sequence**: (1) shell quenching; (2) shell reordering
- Woods-Saxon (WS)/Spin-orbit (SO) gap to Harmonic-oscillator (HO) gap
- **Smooth** in N/Z
- Spin-orbit splitting **reduced**

## SUMMARY :

- **Techniques**
- *Interconnection to production mechanism*
- *Luminosity*
- *Time scale , half life*
- *Spin, excitation energy*
  
- **$N \simeq Z$  -  $^{100}\text{Sn}$**
- *Equivalence  $^{56}\text{Ni}$  -  $^{100}\text{Sn}$*
- *Core excitation in identical  $\pi\nu$  shell*
- *Spin-gap isomers ( $^{98}\text{Cd}, (12^+)$ ;  $^{94}\text{Ag}, (21^+)$ ,  $E_x \simeq 6 \text{ MeV}$ )*
- *Large scale shell model*
  
- **$N \gg Z$  -  $^{68}\text{Ni}$  to  $^{78}\text{Ni}$**
- *Monopole driven shell structure*
- *Weakness of  $N=40$  - persistence of  $N=50$  shell*
- *Disappearance of seniority isomers*
  
- **New shells @  $N \gg Z$**
- *New shells  $N=6, 16(14), 34(32)$  symmetric in isospin*
- *$T=1$  monopole important in  $j=1/2$  shell*

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