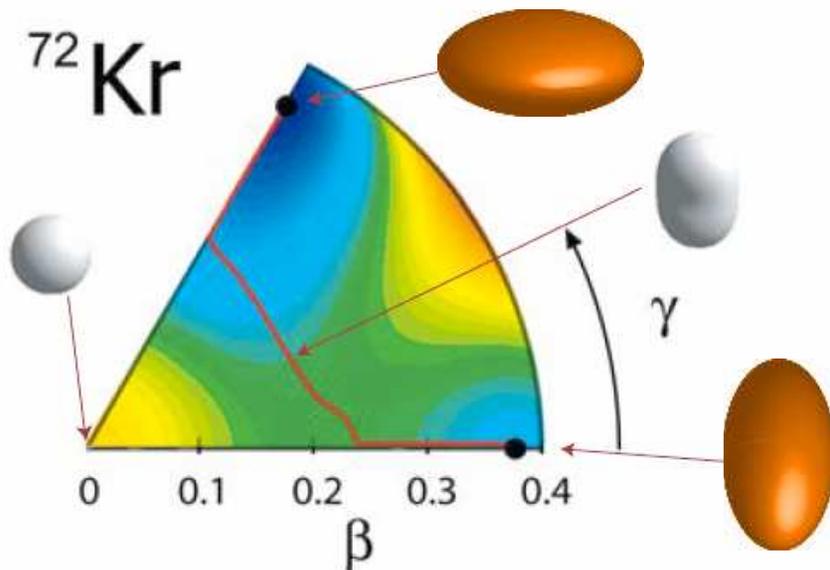


Application of the Adiabatic Self-Consistent Collective Coordinate (ASCC) Method to Shape Coexistence/ Mixing Phenomena



Nobuo Hinohara (Kyoyo)
Takashi Nakatsukasa (RIKEN)
Masayuki Matsuo (Niigata)
Kenichi Matsuyanagi (Kyoto)

Microscopic Description of Nuclear Large-Amplitude Collective Motion by Means of the Adiabatic Self-Consistent Collective Coordinate Method

The major part of this
thesis will appear in
Prog. Theor. Phys.
Jan. 2008
within a few days

Hinohara Nobuo

日野原 伸生

Sunny Field

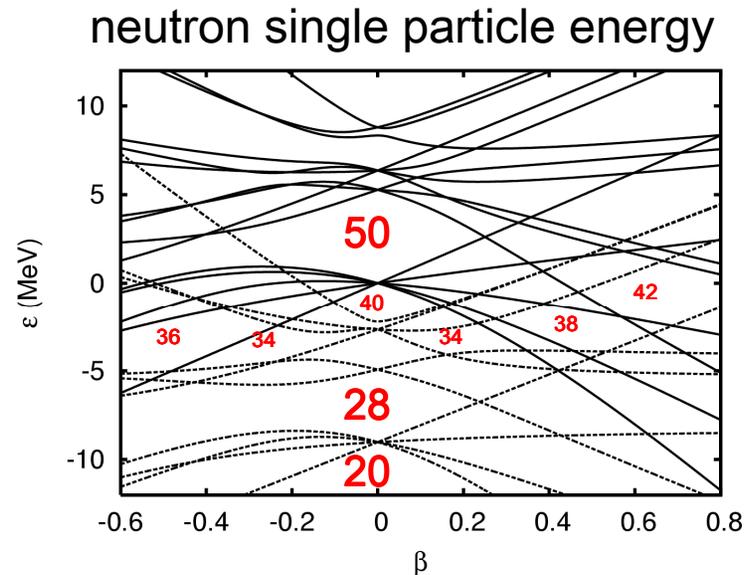
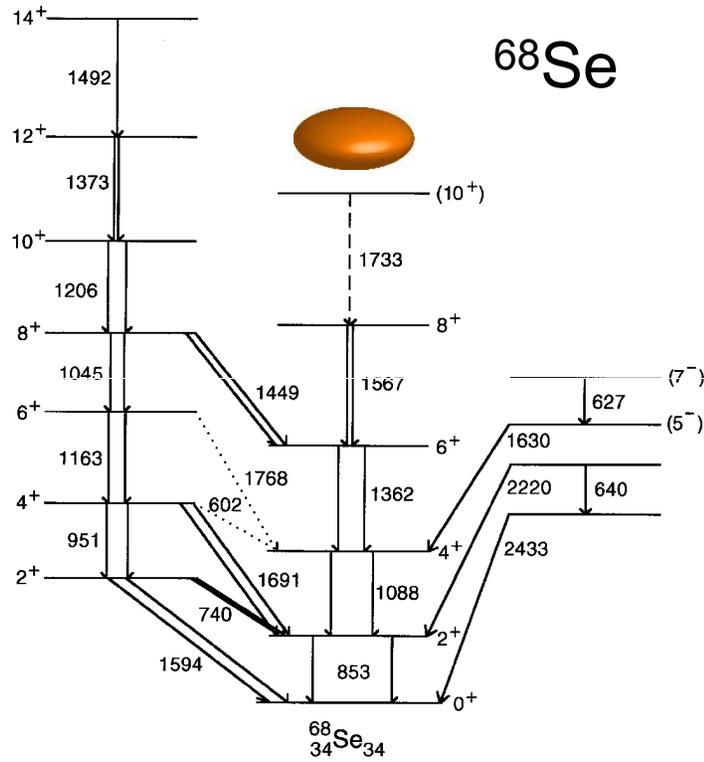
Life lively grows

doctoral dissertation defense

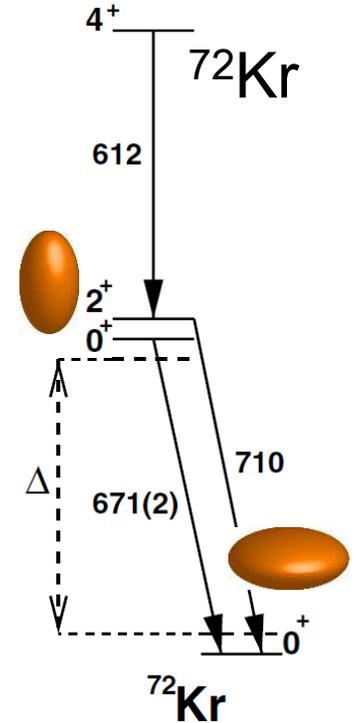
2008.1.17

学位論文公聴会

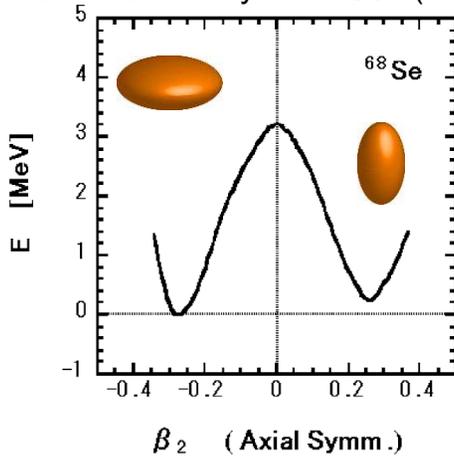
Shape coexistence in N~Z~40 region



Z,N = 34,36 (oblate magic numbers)
 Z,N = 38 (prolate magic number)



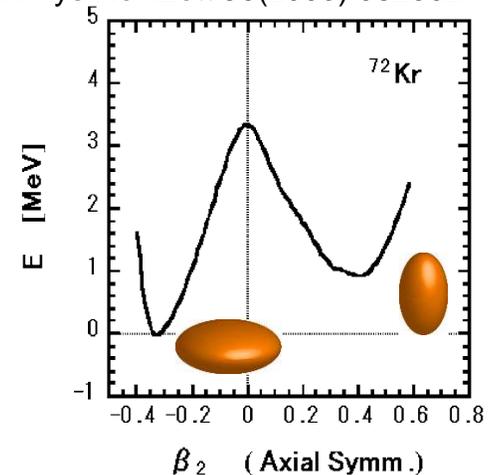
Fischer *et al.* Phys.Rev.C67 (2003) 064318.



- oblate-prolate shape coexistence
- oblate ground state
- shape coexistence/mixing

Skyrme-HFB: Yamagami *et al.* Nucl.Phys.A693 (2001) 579.

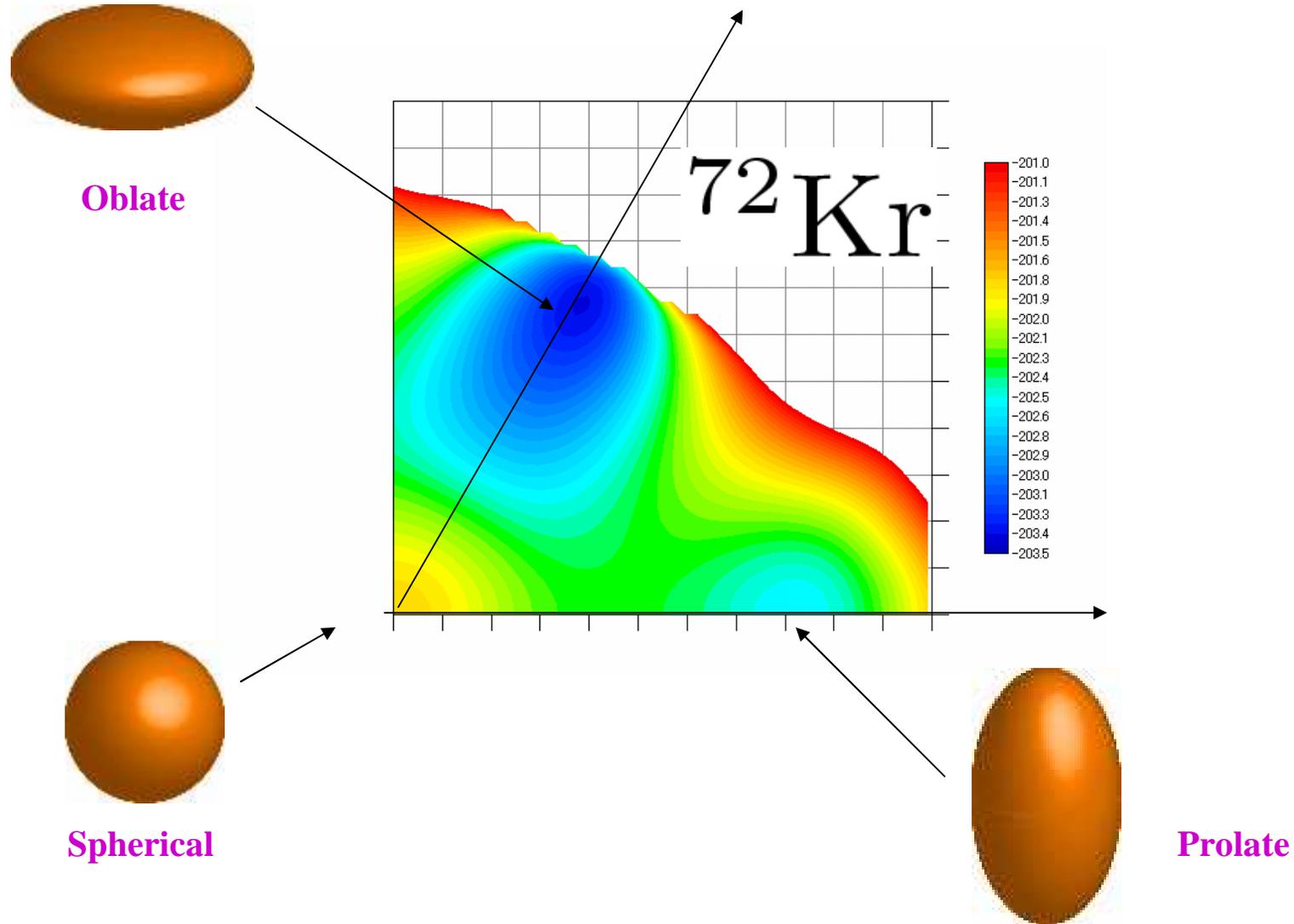
Bouchez *et al.* Phys.Rev.Lett.90(2003) 082502.



Many-Body Tunneling between Different Vacua

Basic question

Why localization is possible for such a low barrier ?!



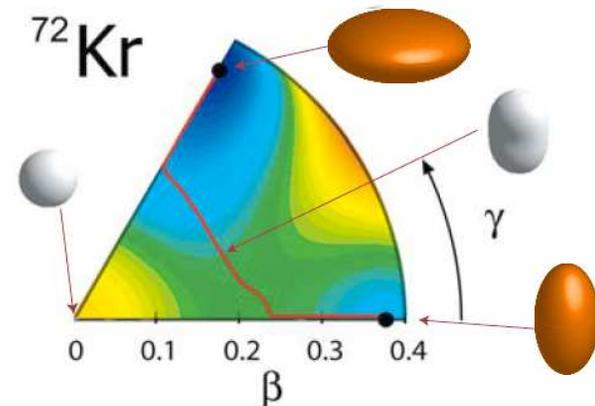
Main points



I am going to report the **first application** of **the microscopic theory of large amplitude collective motion**, based on the **time-dependent mean-field (TDHFB) theory**, to **real nuclear structure phenomena** in nuclei with superfluidity.



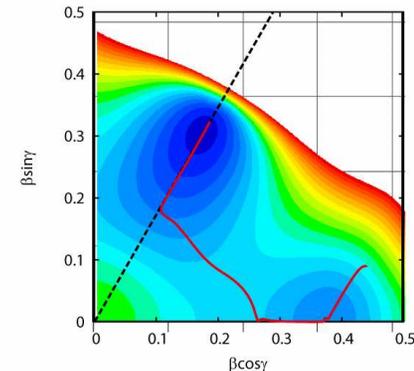
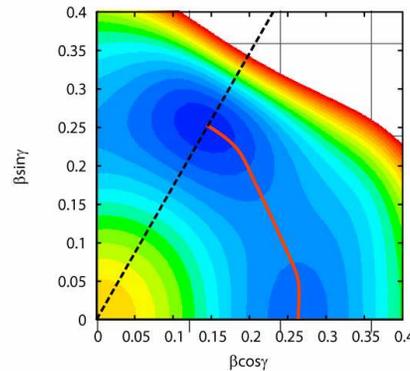
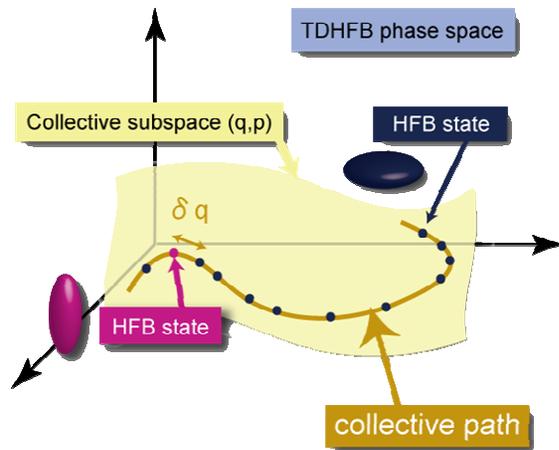
Coexistence/mixing of oblate and prolate shapes is a typical phenomenon of large amplitude collective motion.



Main points



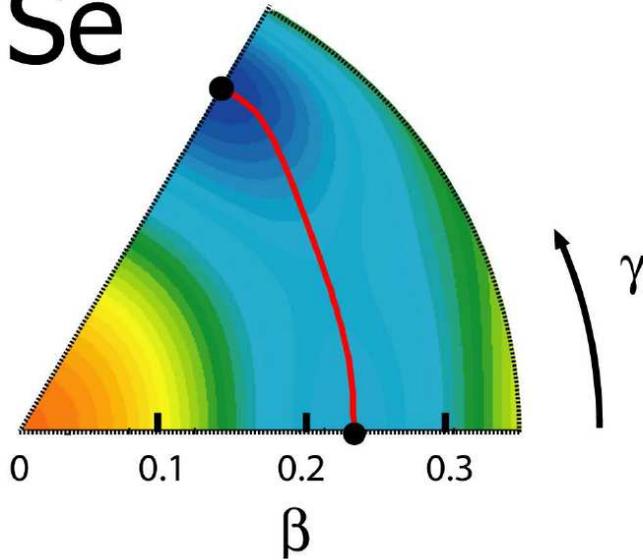
In contrast to the GCM, collective coordinate and momentum are microscopically derived; i.e., self-consistently extracted from huge-dimensional TDHFB phase space.



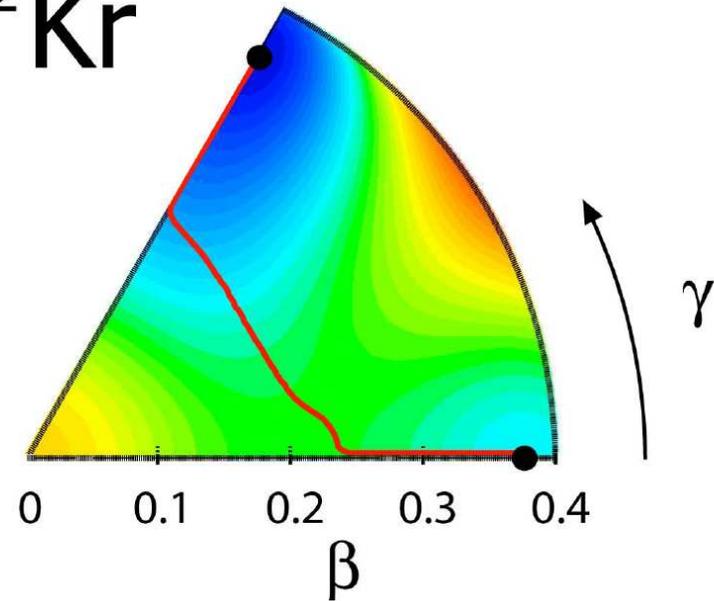
In ^{68}Se and ^{72}Kr , the collective paths, connecting the oblate and prolate minima, run in the triaxially deformed region.

Collective paths obtained by means of the ASCC method

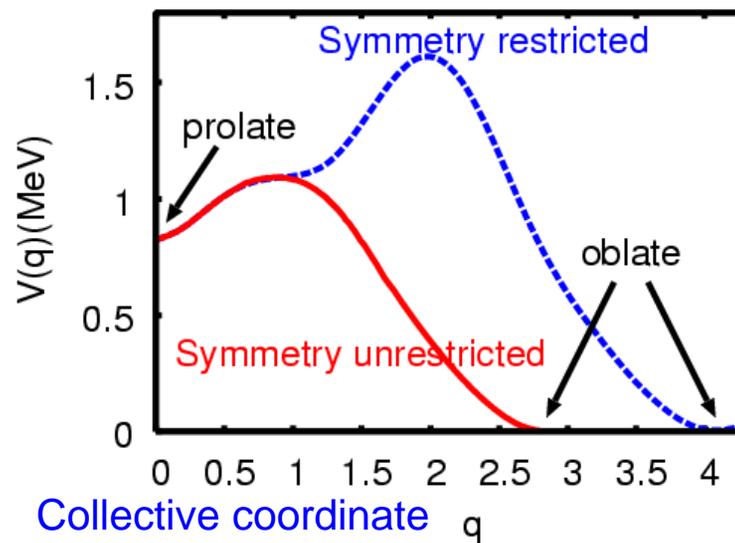
^{68}Se



^{72}Kr



Comparison with the axially symmetric path



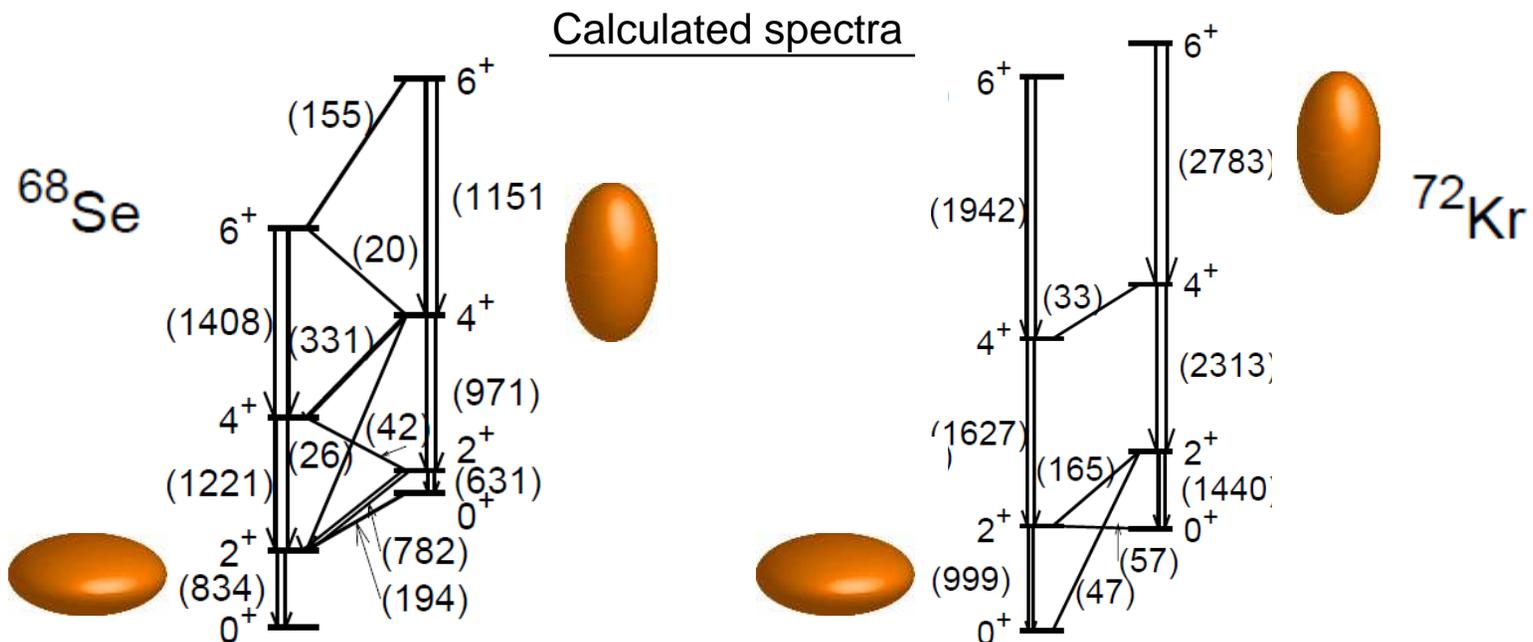
Main points



The collective Hamiltonian, derived microscopically, is quantized and excitation spectra, E2 transitions and quadrupole moments are evaluated for the first time.



The result indicates that the oblate and prolate shapes are strongly mixed at $I=0$, but the mixing rapidly decreases with increasing angular momentum.



After a long history (more than 30 years) ,
 a way for wide applications of large-amplitude theory
 is now open.

$$\delta \langle \phi(q, p) | i\hbar \frac{\partial}{\partial t} - H | \phi(q, p) \rangle = 0.$$

**SCC and
 quasiparticle SCC**

Marumori-Maskawa-Sakata-
 Kuriyama, Yamamura,
 Matsuo, Shimizu-Takada,
 and many colleagues,
 reviewed in
 Prog. Theor. Phys. Supplement
 141 (2001).

**ATDHF and
 ATDHFB**

Villars, Kerman-Koonin, Brink,
 Rowe-Bassermann, Baranger-
 Veneroni,
 Goeke-Reinhard, Bulgac-Klein-Walet,
 Giannoni-Quentin, Dobaczewski-
 Skalski
 and many colleagues, reviewed in
 G. Do Dang, A. Klein and N.R. Walet,
 Phys.

$$|\phi(q, p)\rangle = e^{i\hat{G}(q,p)} |\phi_0\rangle$$

$$\hat{G}(q, p) = \sum G_{mn} (\eta^*)^m \eta^n$$

$$\eta = \frac{1}{\sqrt{2}}(q + ip)$$

$$|\phi(q, p)\rangle = e^{ip\hat{Q}(q)} |\phi(q)\rangle$$

ASCC

Time dependent mean-field

time-dependent
variational principle

$$\delta \langle \phi(q, p) | i\hbar \frac{\partial}{\partial t} - H | \phi(q, p) \rangle = 0.$$

$q + \delta q$

q

collective coordinate q

collective momentum p

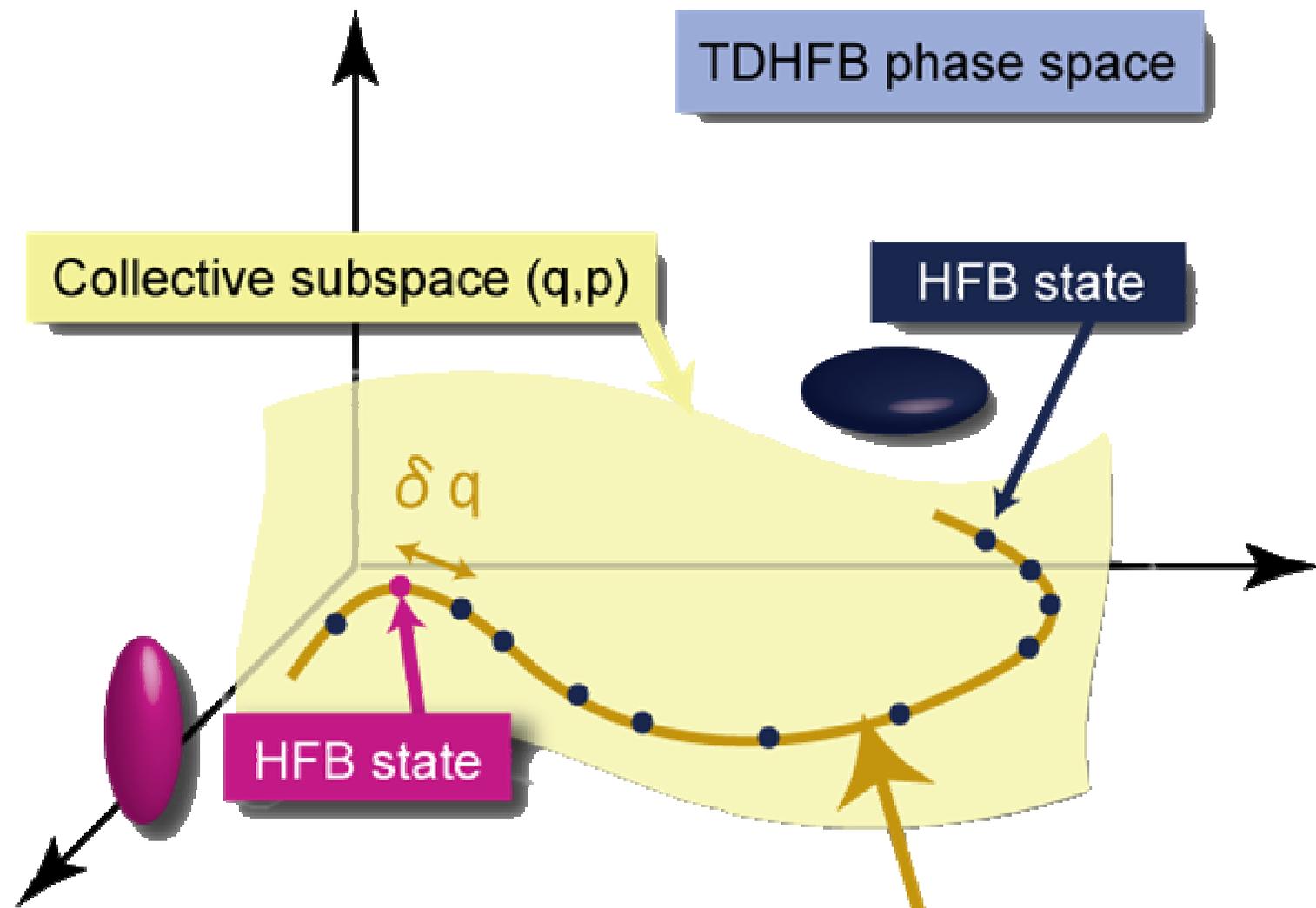
$$\frac{\partial}{\partial t} \Rightarrow \dot{q} \frac{\partial}{\partial q} + \dot{p} \frac{\partial}{\partial p}$$

$$|\phi(q, p)\rangle = e^{ip\hat{Q}(q)} |\phi(q)\rangle$$

Adiabatic expansion
(ATDHFB)

$$|\phi(q + \delta q)\rangle = (1 - i\delta q \hat{P}(q)) |\phi(q)\rangle$$

Find an optimum direction at every point of q



$$\delta \langle \phi(q, p) | i\hbar \frac{\partial}{\partial t} - H | \phi(q, p) \rangle = 0.$$

$$|\phi(q, p)\rangle = e^{ip\hat{Q}(q)} |\phi(q)\rangle$$

$$|\phi(q + \delta q)\rangle = (1 - i\delta q \hat{P}(q)) |\phi(q)\rangle$$

collective path

ASCC Basic Equations

Moving-frame HFB equation

$$\delta \langle \phi(q) | \hat{H}_M(q) | \phi(q) \rangle = 0$$

(from 0-th order in p)

moving-frame Hamiltonian

$$\hat{H}_M(q) = \hat{H} - \lambda(q)\hat{N} - \frac{\partial V}{\partial q} \hat{Q}(q)$$

Local harmonic equations (moving-frame QRPA equations)

Not included in HFB

$$\delta \langle \phi(q) | [\hat{H}_M(q), \hat{Q}(q)] - \frac{1}{i} B(q) \hat{P}(q) | \phi(q) \rangle = 0 \quad (\text{from 1st-order in p})$$

$$\delta \langle \phi(q) | [\hat{H}_M(q), \frac{1}{i} \hat{P}(q)] - C(q) \hat{Q}(q) - \frac{\partial \lambda}{\partial q} \hat{N} | \phi(q) \rangle = 0 \quad (\text{from 2nd-order in p})$$

$$-\frac{1}{2B(q)} [[\hat{H}_M(q), (\hat{H} - \lambda(q)\hat{N})_{aa, a^\dagger a^\dagger \text{ part}}], \hat{Q}(q)] | \phi(q) \rangle = 0$$

Terms not included in QRPA

$$C(q) = \frac{\partial^2 V}{\partial q^2} + \frac{1}{2B(q)} \frac{\partial B}{\partial q} \frac{\partial V}{\partial q}$$

$$\hat{P}(q) | \phi(q) \rangle = i \frac{\partial}{\partial q} | \phi(q) \rangle$$

Collective Hamiltonian

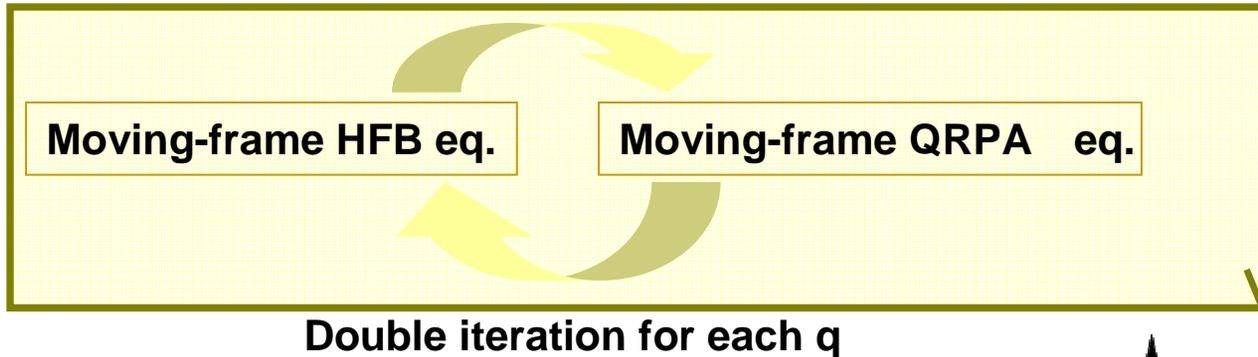
$$\begin{aligned} \mathcal{H}(q, p, N) &= \langle \phi(q, p, N) | \hat{H} | \phi(q, p, N) \rangle \\ &= V(q) + \frac{1}{2} B(q) p^2 + \lambda(q) n \end{aligned}$$

Canonical variable conditions

$$\begin{cases} \langle \phi(q) | [\hat{Q}(q), \hat{P}(q)] | \phi(q) \rangle = i \\ \langle \phi(q) | [\hat{\Theta}(q), \hat{N}] | \phi(q) \rangle = i \end{cases}$$

Basic Scheme of the ASCC method (1)

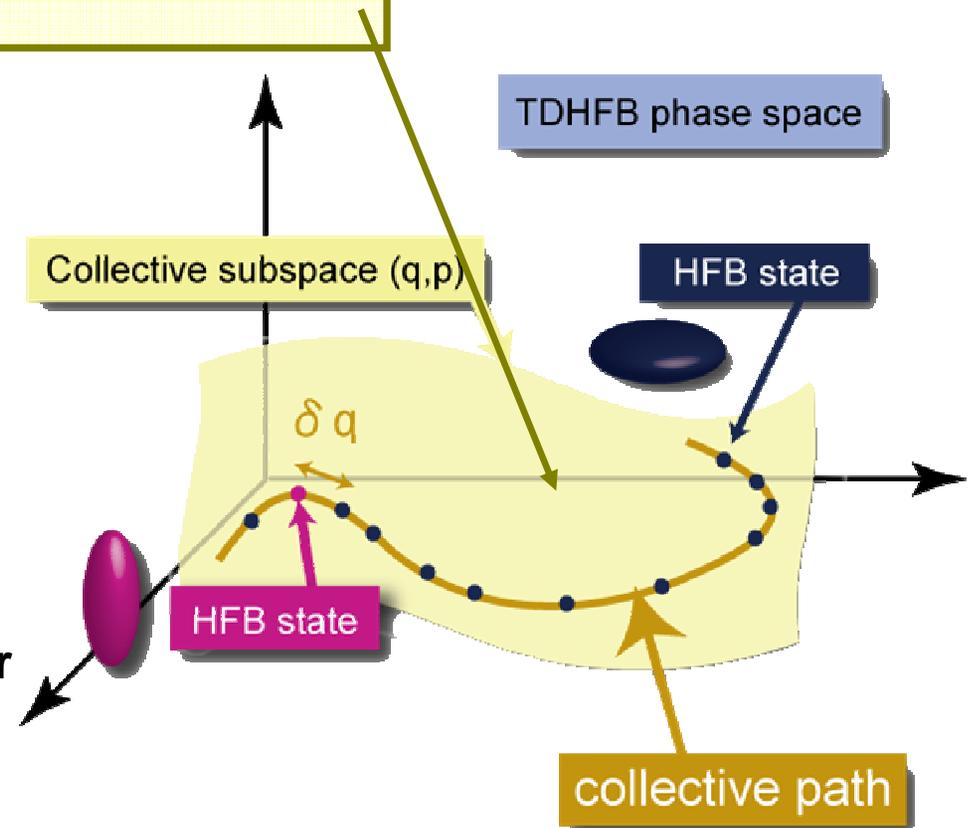
1st Step: Solve ASCC equations and find collective path.



$$\mathcal{H}(q, p, \mathbf{I}) = \frac{1}{2} B(q) p^2 + V(q) + \sum_{i=1}^3 \frac{I_i^2}{2 \mathcal{J}_i(q)}$$

collective mass collective potential

Thouless-Valatin Moment of Inertia for moving-frame Hamiltonian



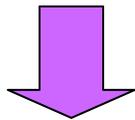
An important remark

The ASCC method was proposed in

M. Matsuo, T. Nakatsukasa and K. Matsuyanagi ,
Prog. Theor. Phys. 103 (2000) 959.

Quite recently, it was found that its basic equations are **invariant against gauge transformations** associated with **pairing correlations**.

$$|\phi(q, p, \varphi, n)\rangle = e^{-i\varphi\tilde{N}} e^{ip\hat{Q}(q)} e^{in\hat{\Theta}(q)} |\phi(q)\rangle$$



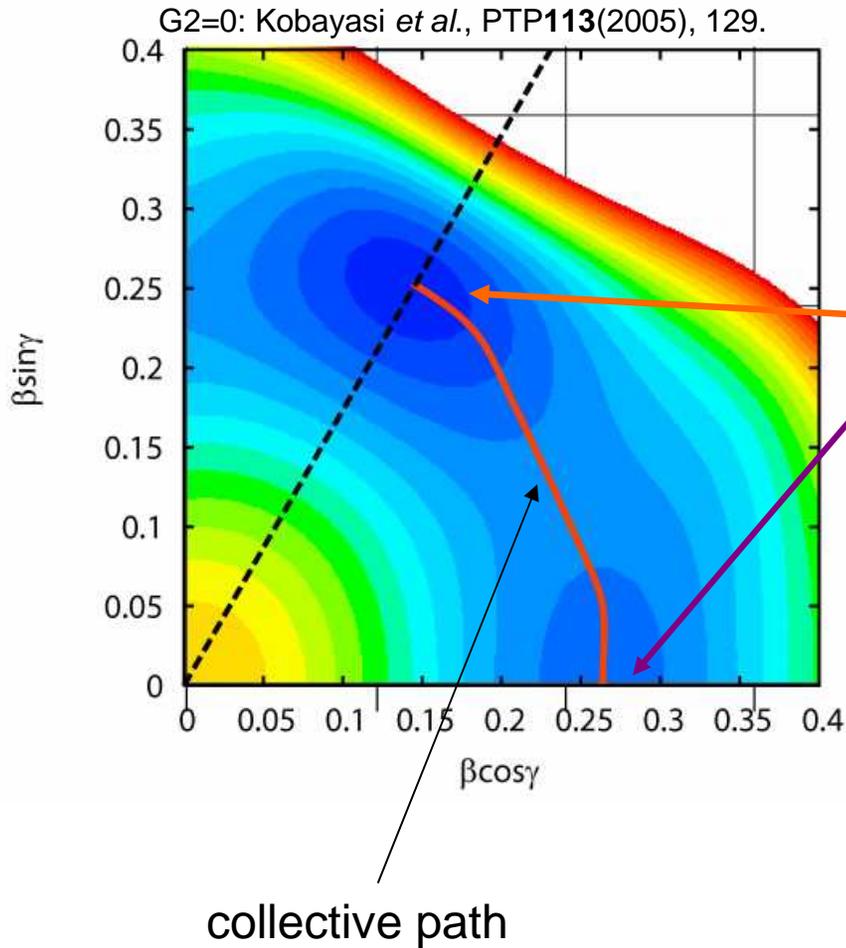
Gauge invariant ASCC method.

Choosing an appropriate **gauge fixing condition**,
numerical instabilities encountered previously
are now completely removed.

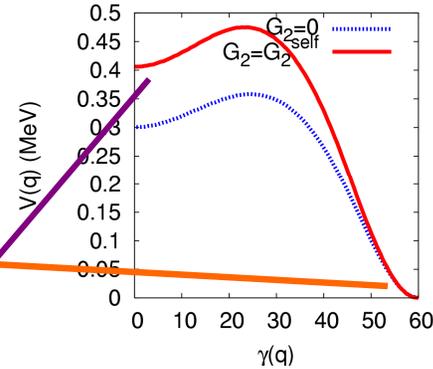
N. Hinohara et al., Prog. Theor. Phys. 117 (2007) 451

Collective path in ^{68}Se

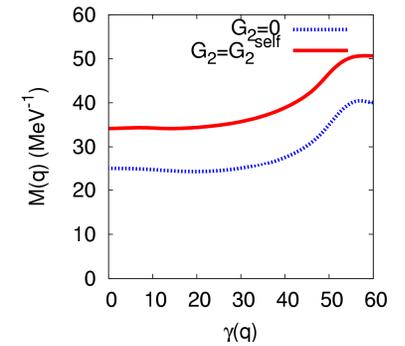
P0+P2+QQ interaction



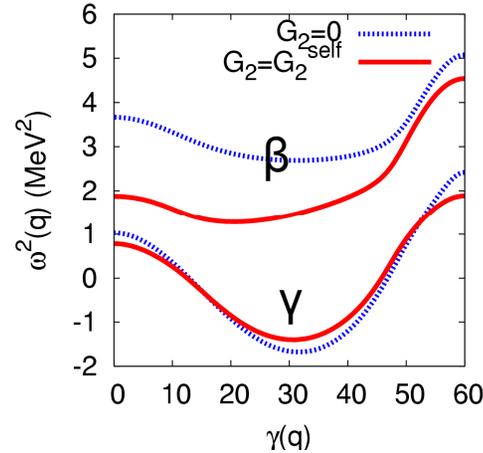
Collective potential



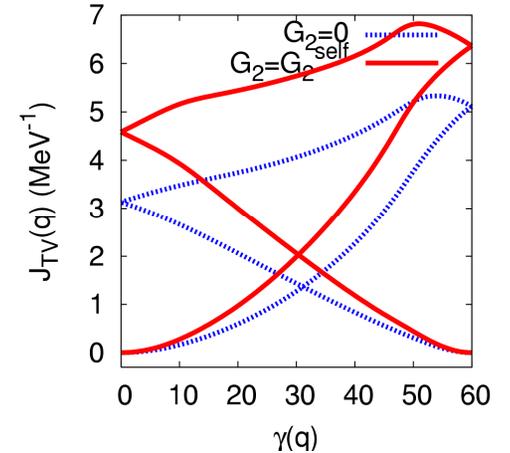
Collective mass



Moving-frame QRPA frequency



Moment of Inertia



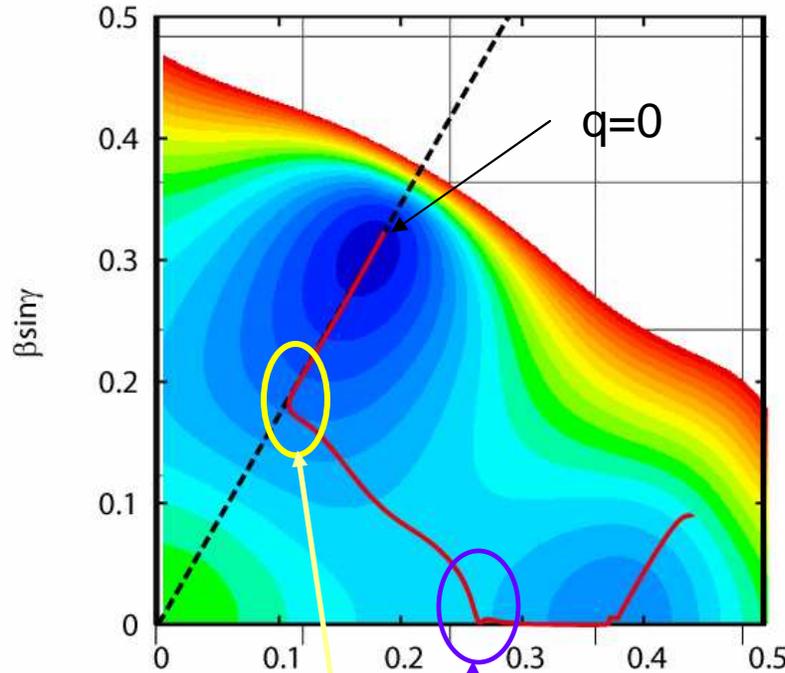
- Triaxial deformation connects two local minima
- Enhancement of the collective mass and Mol by the quadrupole pairing

↑
due to the time-odd pair field

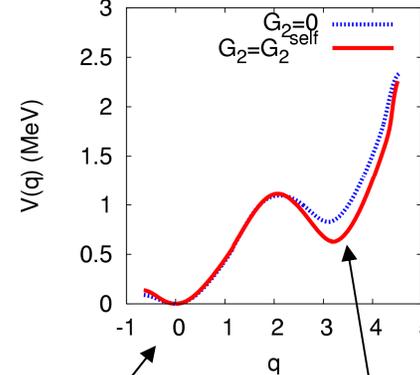
Collective path in ^{72}Kr

P0+P2+QQ interaction

$G_2=0$: Kobayasi *et al.*, PTP113(2005), 129.



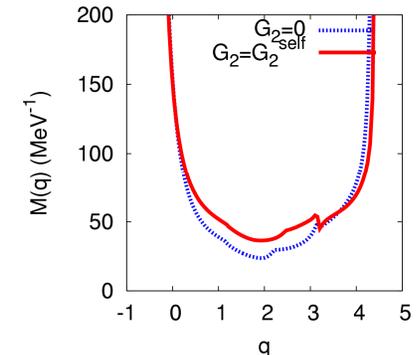
Collective potential



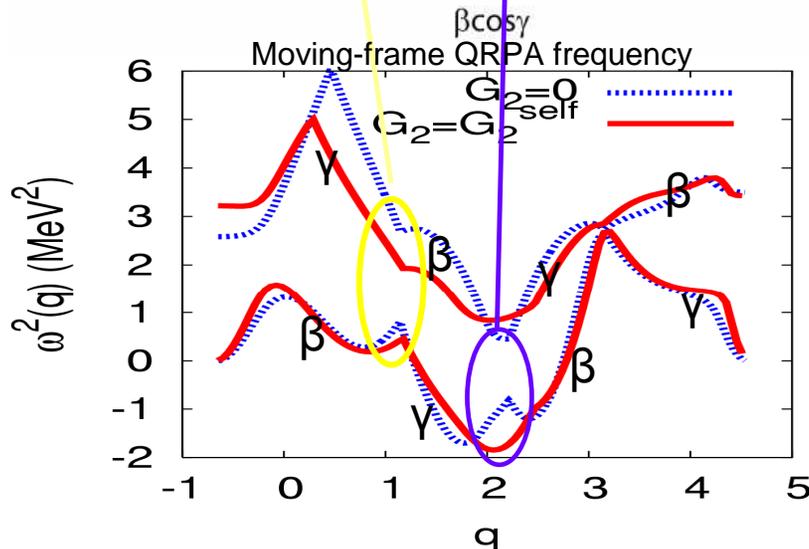
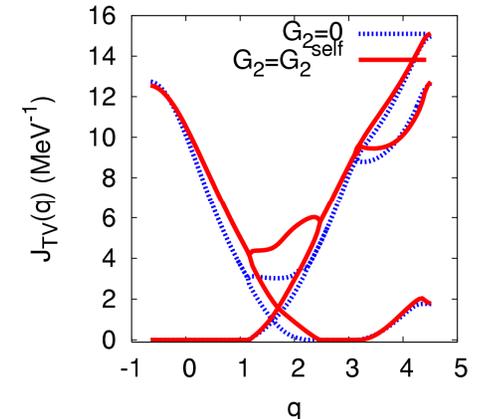
oblate

prolate

Collective mass



Moment of Inertia



- Dynamical symmetry breaking of the path
- Triaxial degrees of freedom: important
- Enhancement of the collective mass and Mol by the quadrupole pairing

Basic Scheme of the ASCC Method (2)

2nd Step: Requantize the collective Hamiltonian.

$$p \rightarrow \frac{\hbar}{i} \frac{\partial}{\partial q}, \quad I_i \rightarrow \hat{I}_i,$$

Collective wave function

vibrational wave functions

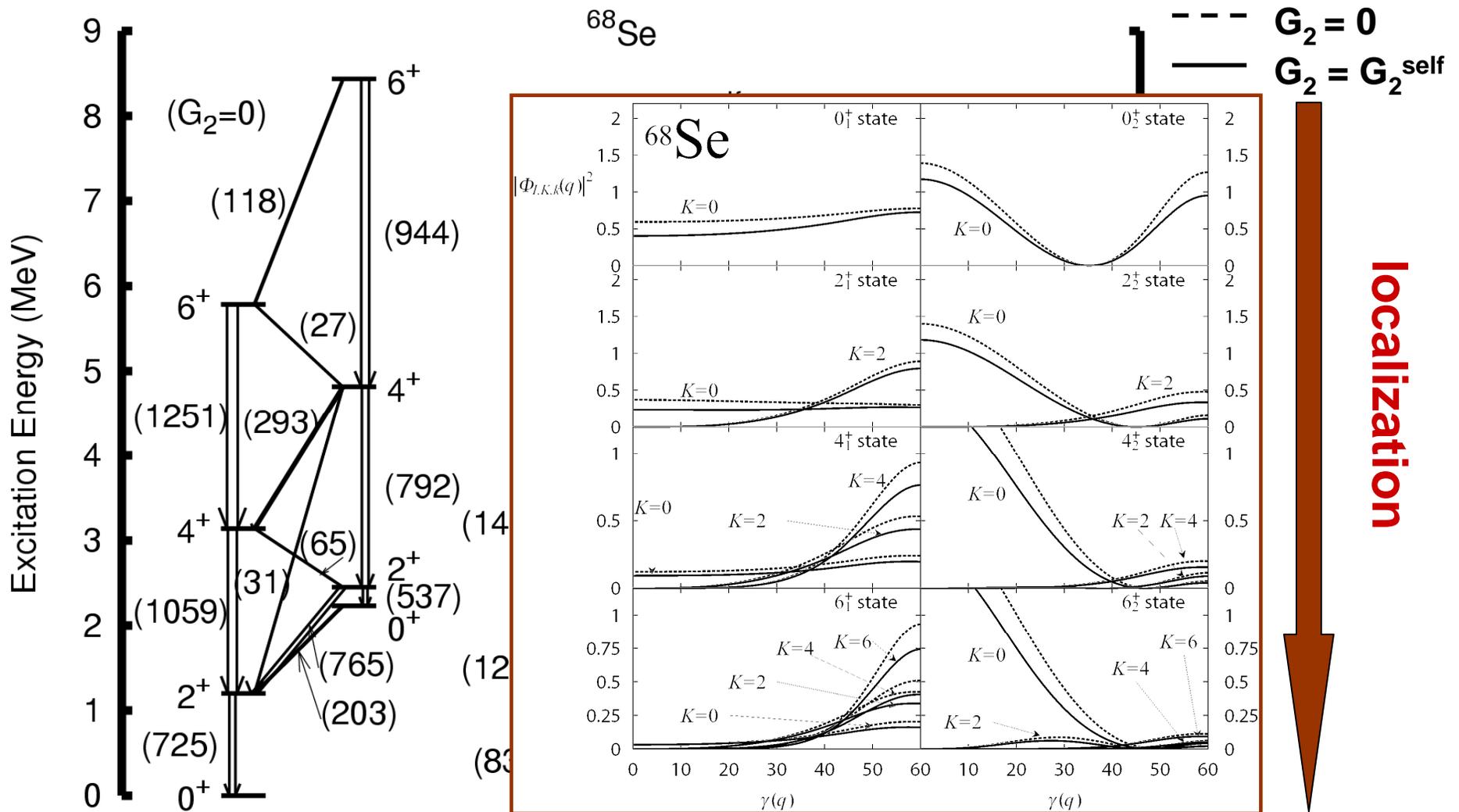
$$\begin{aligned} \Psi_{IMk}(q, \Omega) &= \sum_{K=-I}^I \Phi'_{IKk}(q) \sqrt{\frac{2I+1}{8\pi^2}} \mathcal{D}_{MK}^I(\Omega) \\ &= \sum_{K=0}^I \Phi_{IKk}(q) \langle \Omega | IMK \rangle. \end{aligned}$$

rotational wave functions

Collective Schrodinger eq.

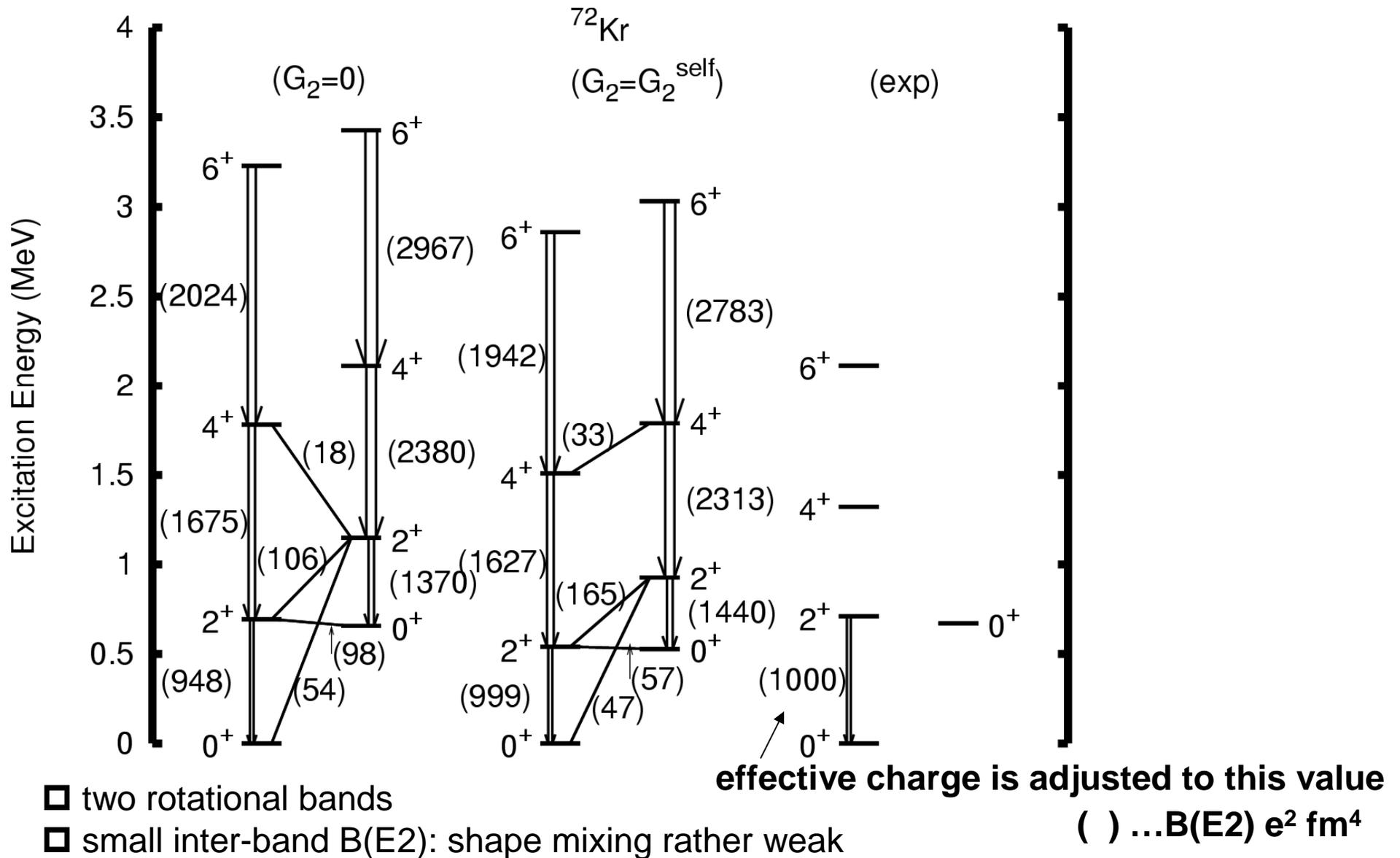
$$\left(-\frac{1}{2} \frac{\partial^2}{\partial q^2} + \sum_{i=1}^3 \frac{\hat{I}_i^2}{2\mathcal{J}_i(q)} + V(q) \right) \Psi_{IMk}(q, \Omega) = E_{I,k} \Psi_{IMk}(q, \Omega)$$

Collective wave functions in ^{68}Se



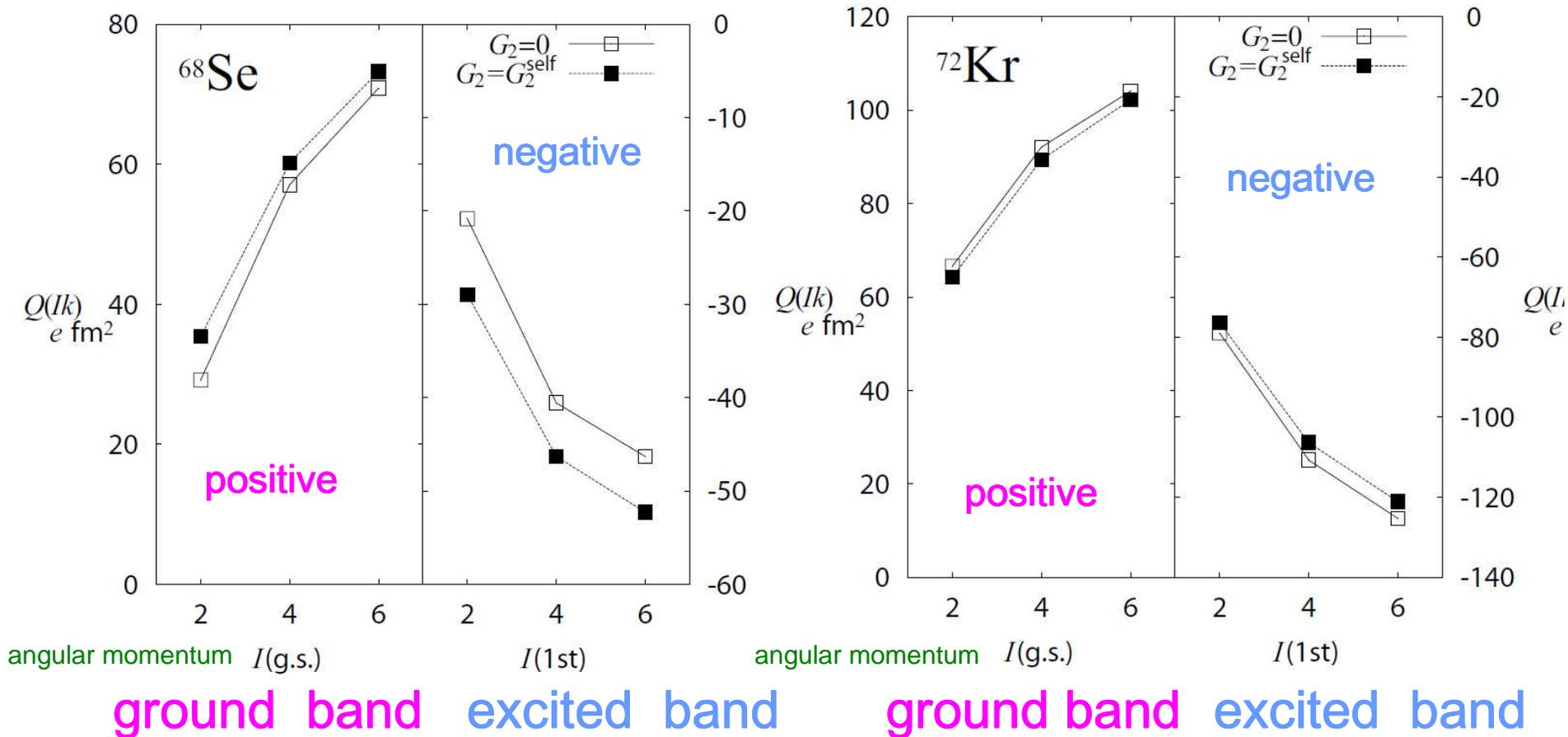
- $I = 0$: oblate and prolate shapes are strongly mixed via triaxial degree of freedom
- ground band: mixing of different K components, excited band: $K=0$ dominant
- oblate-prolate mixing: strong in 0^+ states, decreases as angular momentum increases

Excitation Spectra of ^{72}Kr



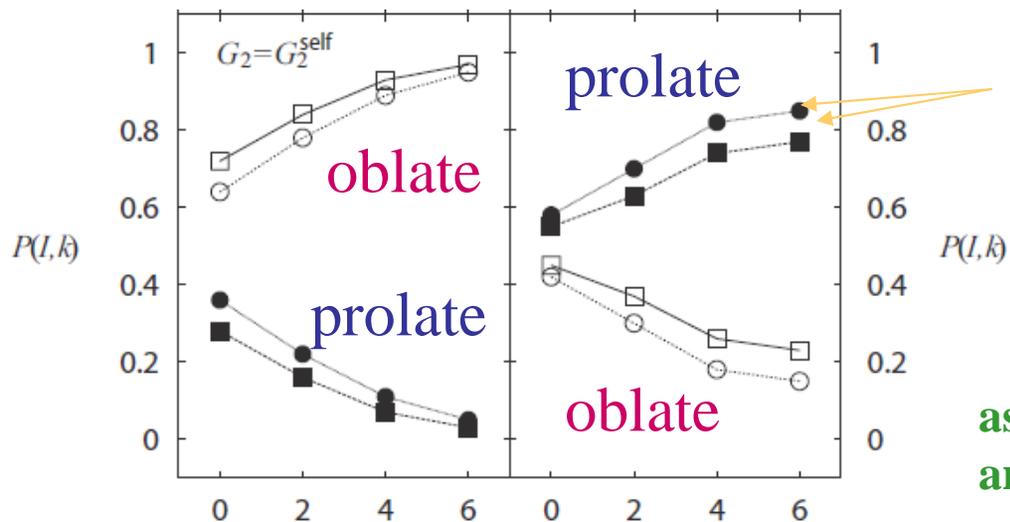
EXP : Fischer et al., Phys.Rev.**C67** (2003) 064318, Bouchez, et al., Phys.Rev.Lett.90 (2003) 082502.
 Gade, et al., Phys.Rev.Lett.**95** (2005) 022502, **96** (2006) 189901

Spectroscopic quadrupole moments



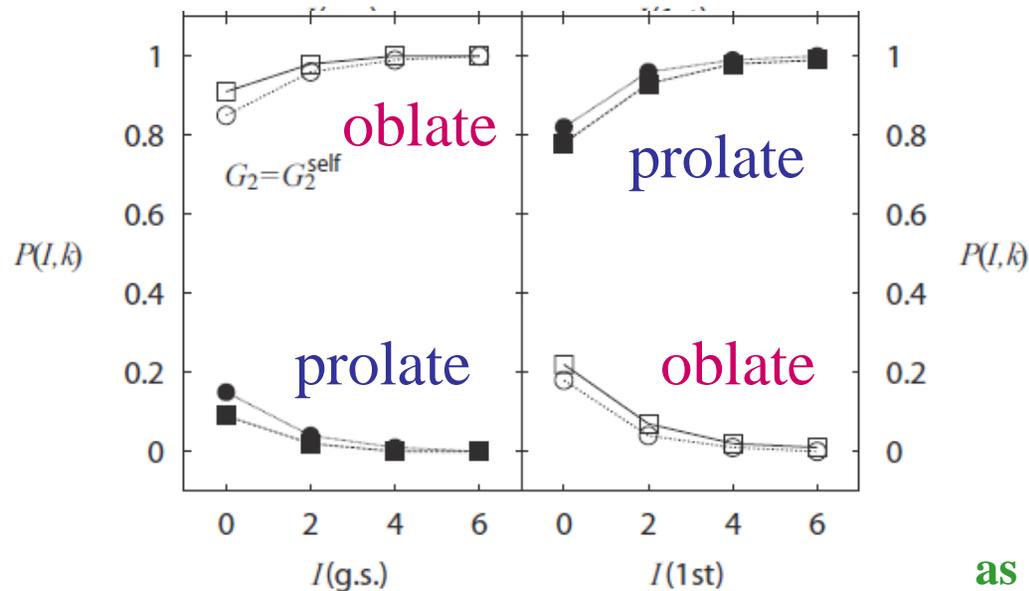
Probabilities of the Oblate and Prolate Components

^{68}Se



as a function of angular momentum

^{72}Kr



as a function of angular momentum

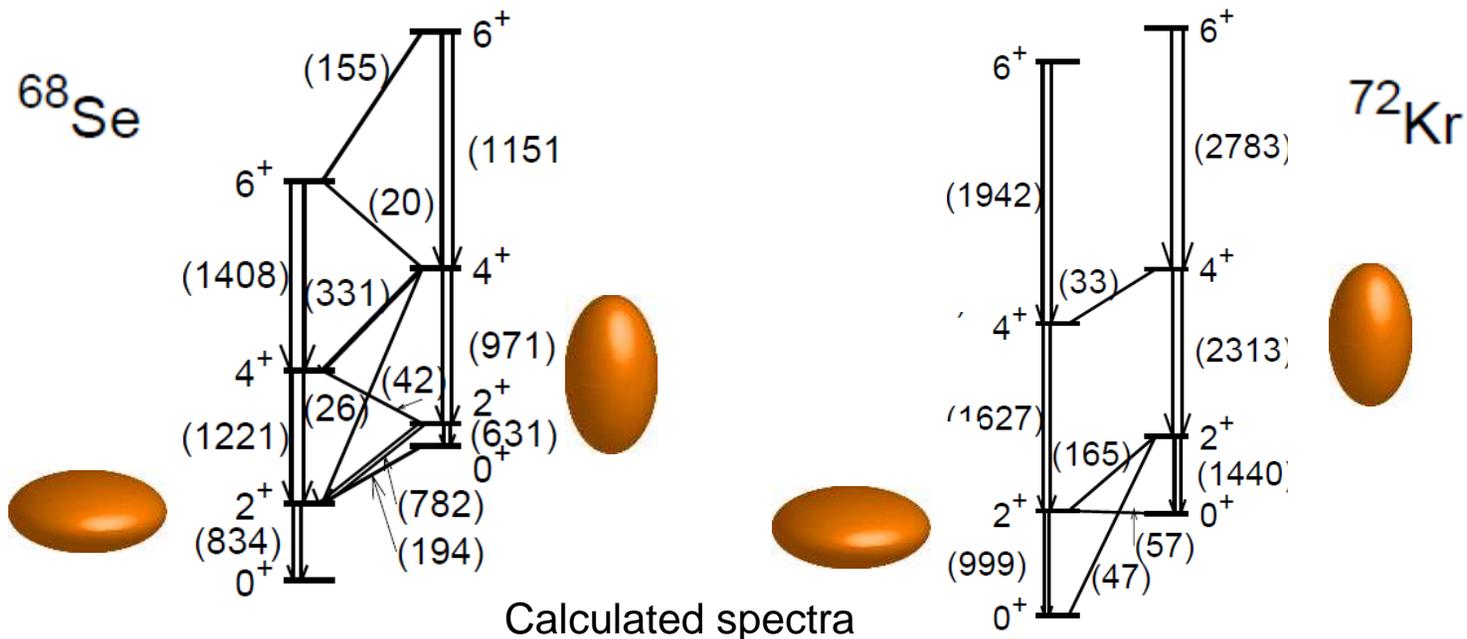
ground band

excited band

Summary

For the first time, excitation spectra and E2 properties were evaluated quantizing the collective Hamiltonian derived by the ASCC method

The result indicates interesting properties of the oblate-prolate shape mixing dynamics, like decline of mixing with increasing angular momentum.



Wide applications can be envisaged in the coming years